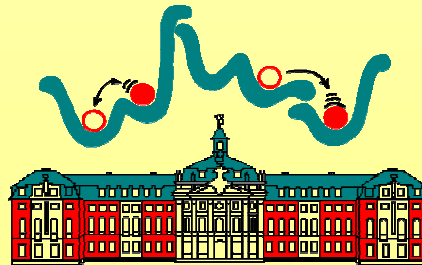


# Application of Linear, Nonlinear and Nanoscale Conductivity Spectroscopy for Characterising Ion Transport in Solid Electrolytes

Bernhard Roling

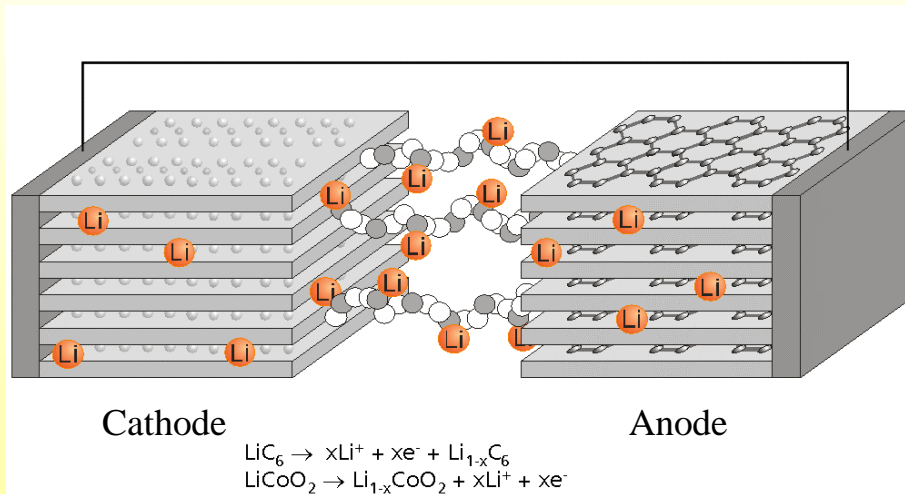
Institute of Physical Chemistry  
and Collaborative Research Center 458  
Westfälische Wilhelms-Universität Münster  
Germany



# Fast ion conductors (superionic conductors):

Solid materials with conductivity  $> 10^{-3}$  S/cm at room temperature

## Areas of application:

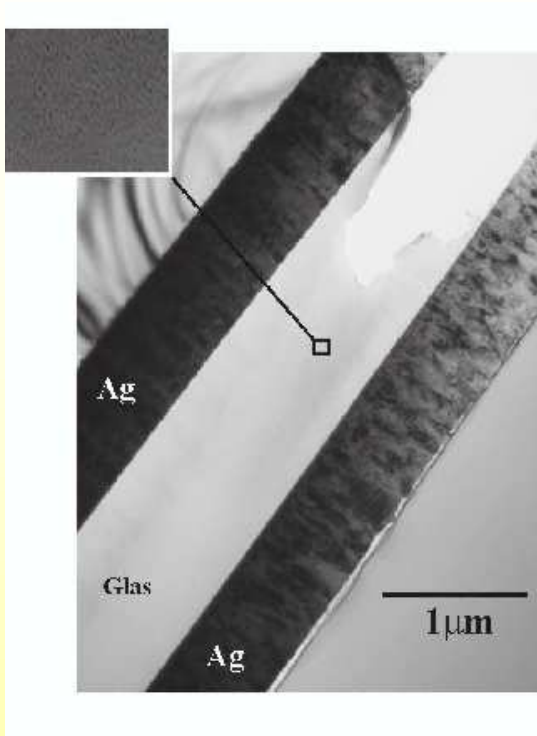


Lithium batteries



Electrochromic windows

## Thin films



F. Berkemeier, G. Schmitz,  
University of Münster 2005

### *Preparation:*

- RF magnetron sputtering
- Sol-gel methods and spin coating

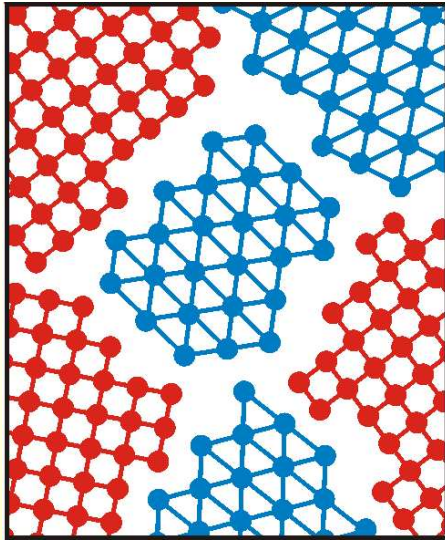
### *Goals:*

- Thickness of the order of 100 nm
- High chemical, electrochemical and mechanical stability
- Conductivity:  $10^{-5} - 10^{-4}$  S/cm

High electric fields:  $5 \text{ V} / 100 \text{ nm} = 500 \text{ kV/cm} !$

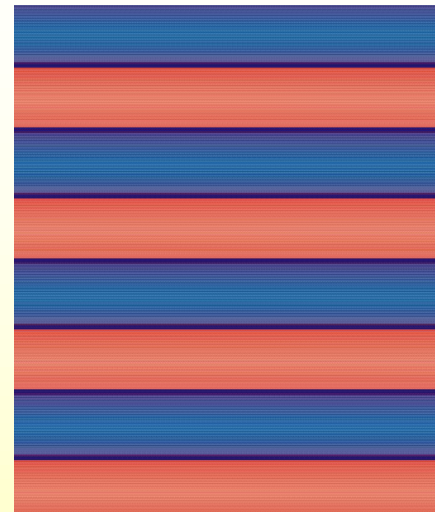
→ Field-dependent ionic conductivity

# Nano- and mesostructured ionic conductors



P. Heitjans, S. Indris,  
*Phys. Cond. Mat.*  
**15** (2003) R1257.

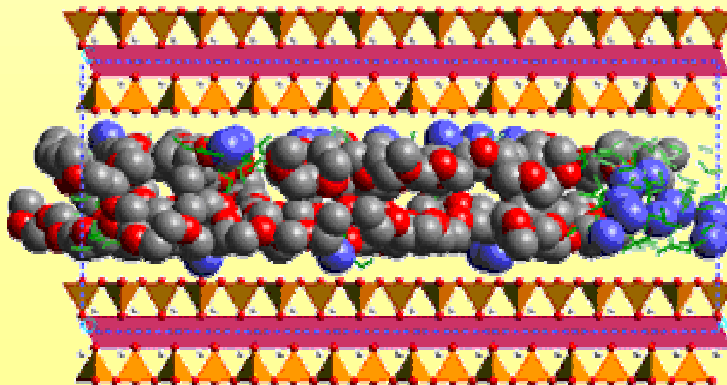
**Conductor-Insulator**  
nanocomposites



$\text{CaF}_2$   
 $\text{BaF}_2$   
 $\text{CaF}_2$   
 $\text{BaF}_2$   
 $\text{CaF}_2$   
 $\text{BaF}_2$   
 $\text{CaF}_2$   
 $\text{BaF}_2$

N. Sata et al.  
*Nature* **408**  
(2000) 946

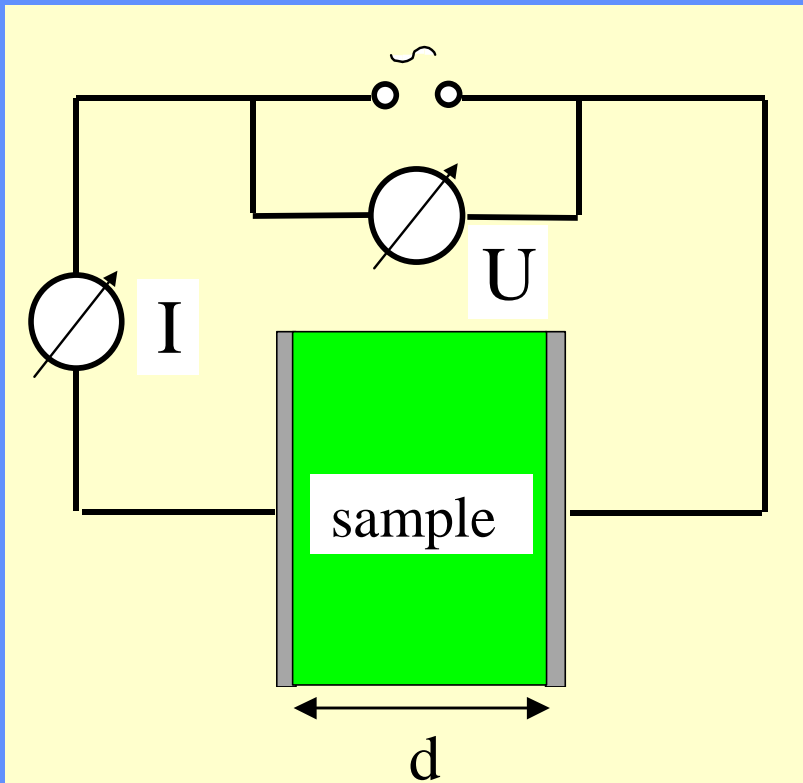
Heterolayered  
conductors



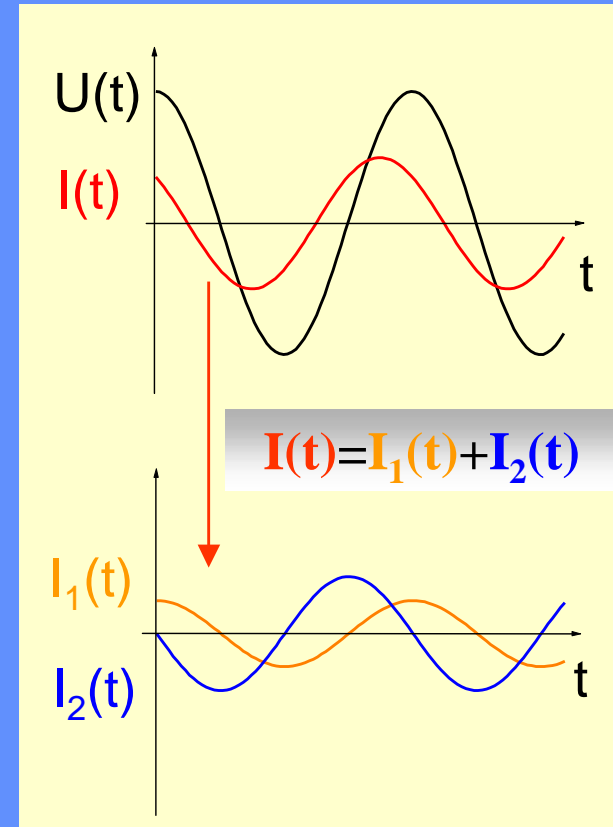
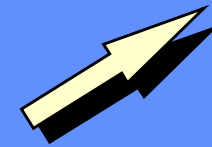
Nanogel electrolytes

M. M. E. Jacob et al.,  
*J. Mat. Chem.* **13** (2004) 1.

# 1. Linear Conductivity Spectroscopy



$A$  = contact area between sample and electrodes



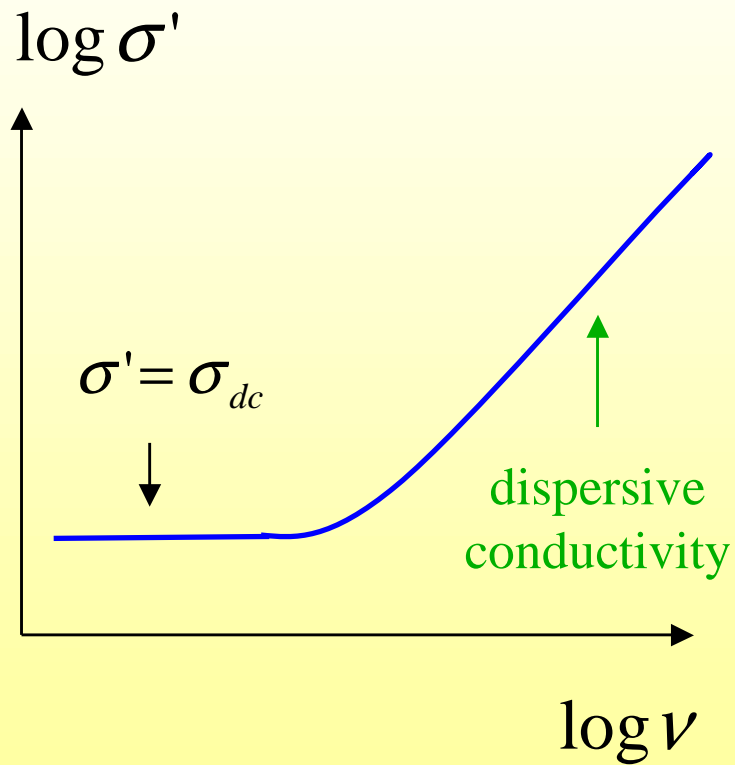
$$\sigma'(\omega) = (I_{0,1}/U_0) * (d/A)$$

Measure for **dissipated** electrical energy

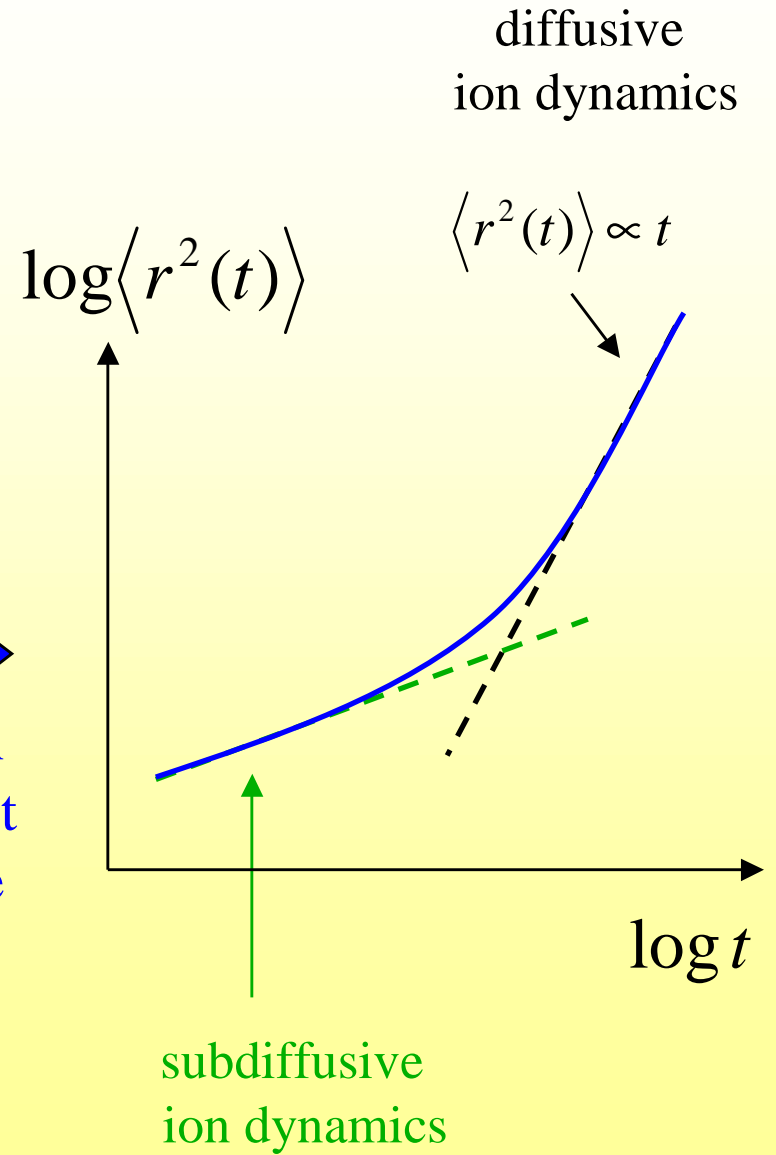
$$\sigma''(\omega) = (I_{0,2}/U_0) * (d/A)$$

Measure for **stored** electrical energy

# Linear response theory

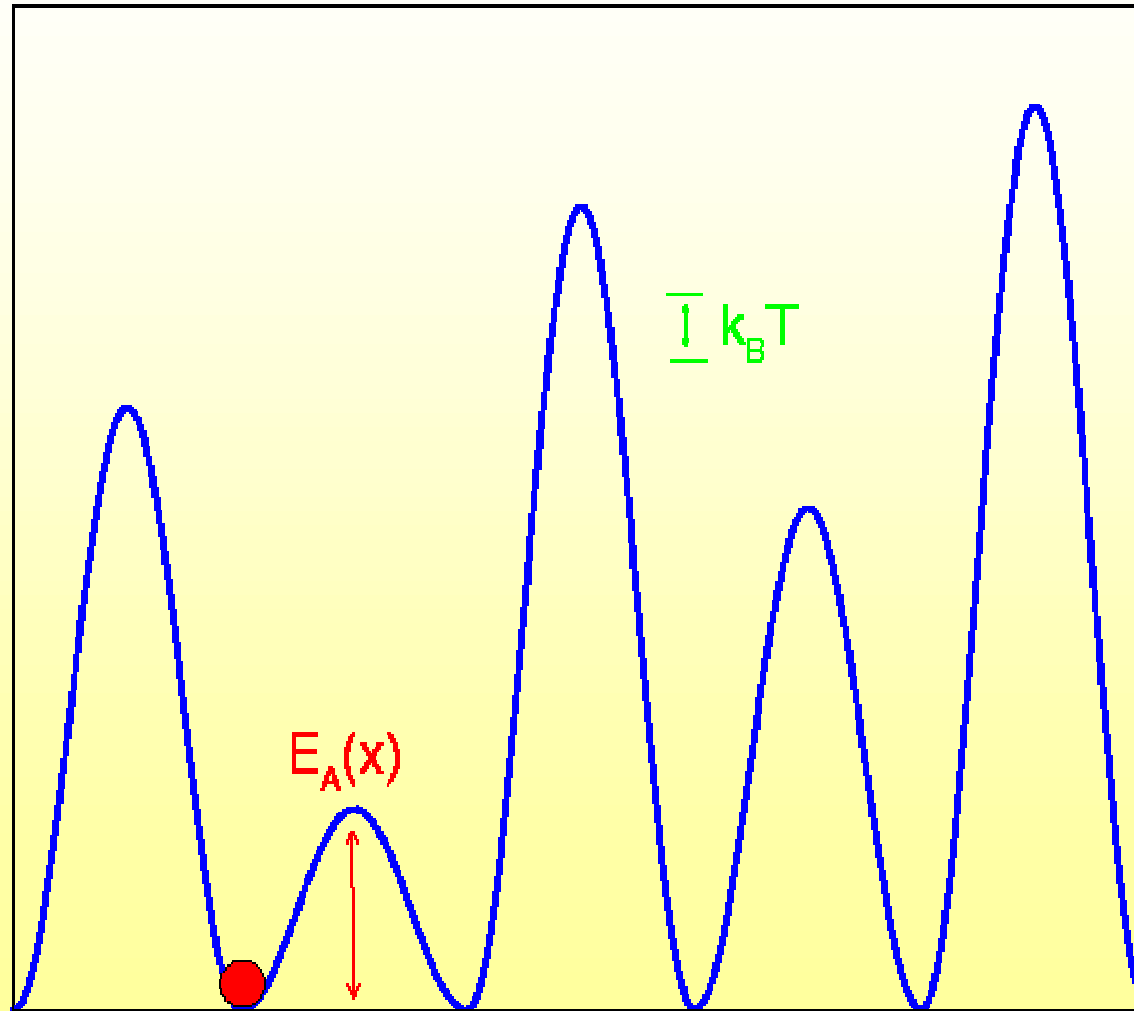


Linear response theory  
Diffusion coefficient of mobile ions

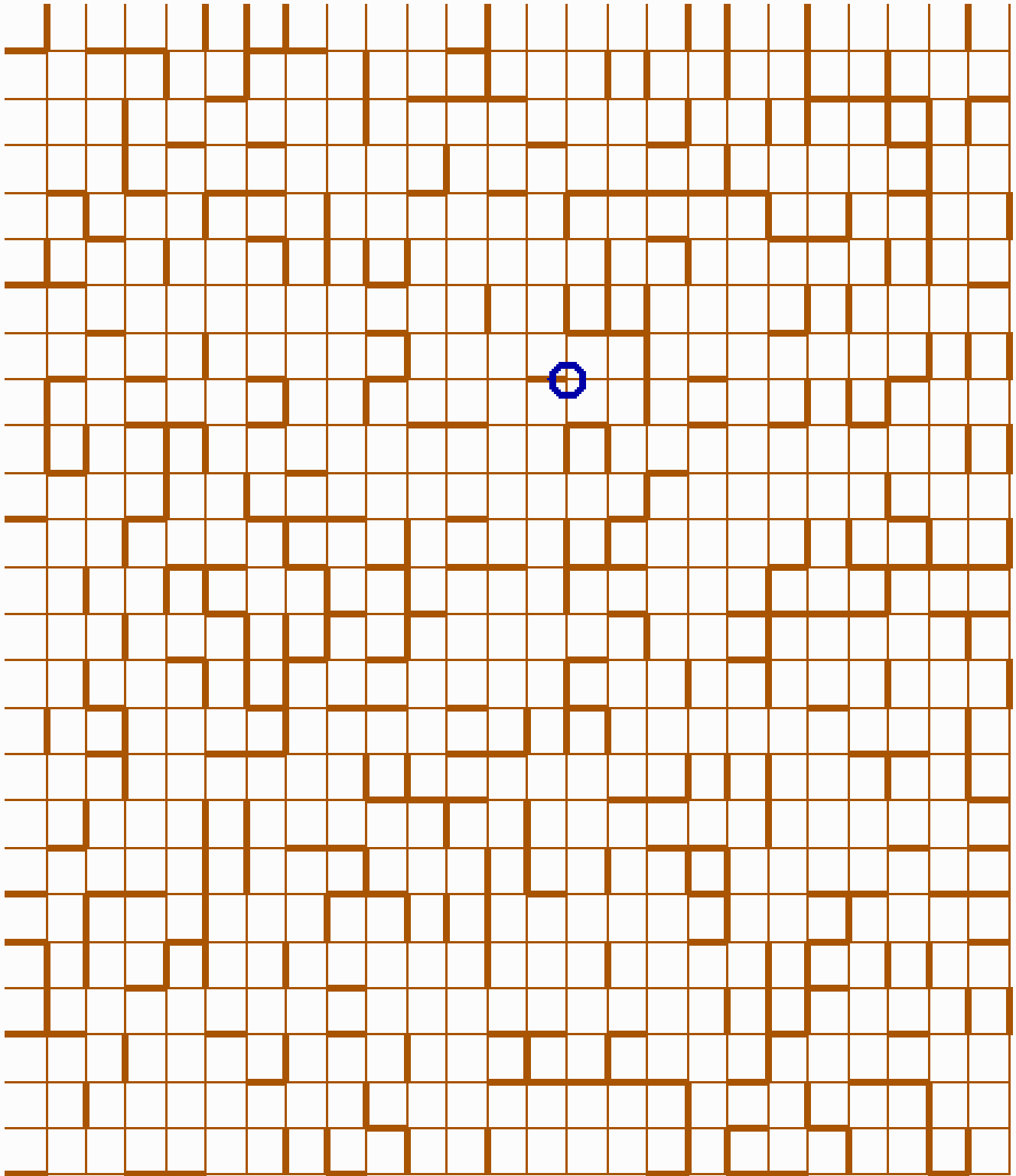


# Random barrier model

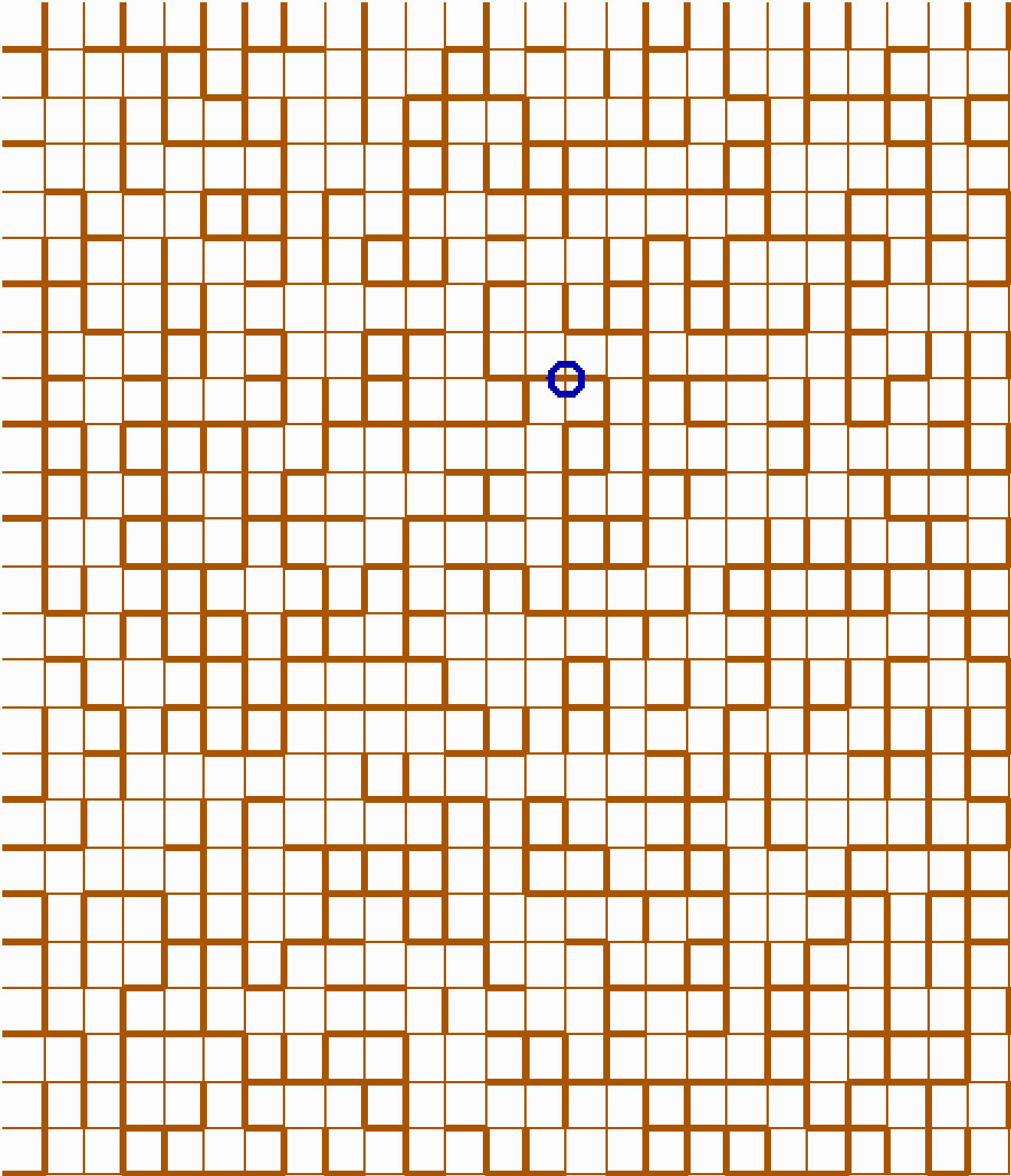
Potential  
energy  
 $V$



space coordinate  $x$







# Spectra of Ion Conducting Glasses

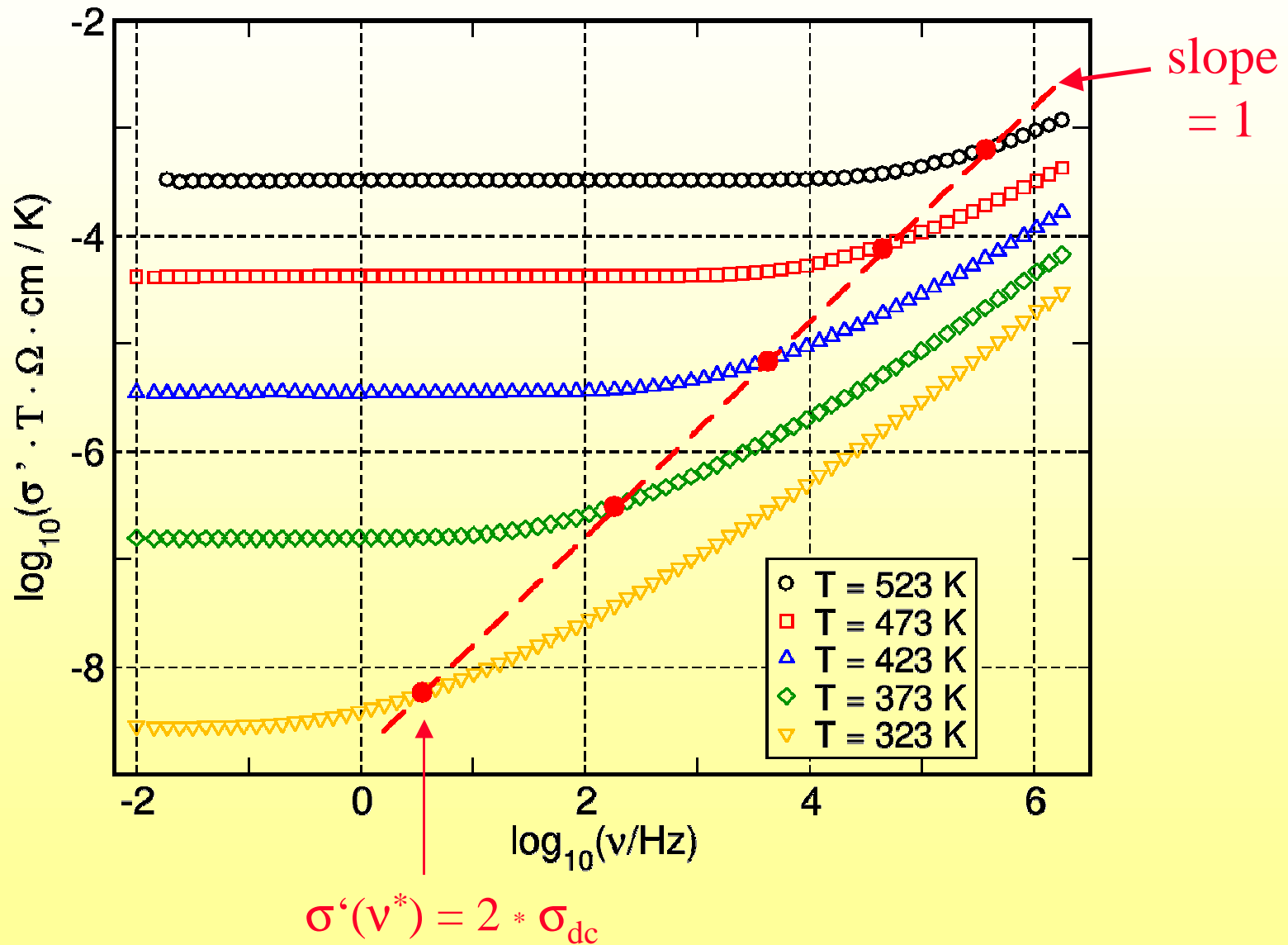
Variation of compositional parameters:

- Number density of mobile ions
- Structure of glass network (solid matrix)

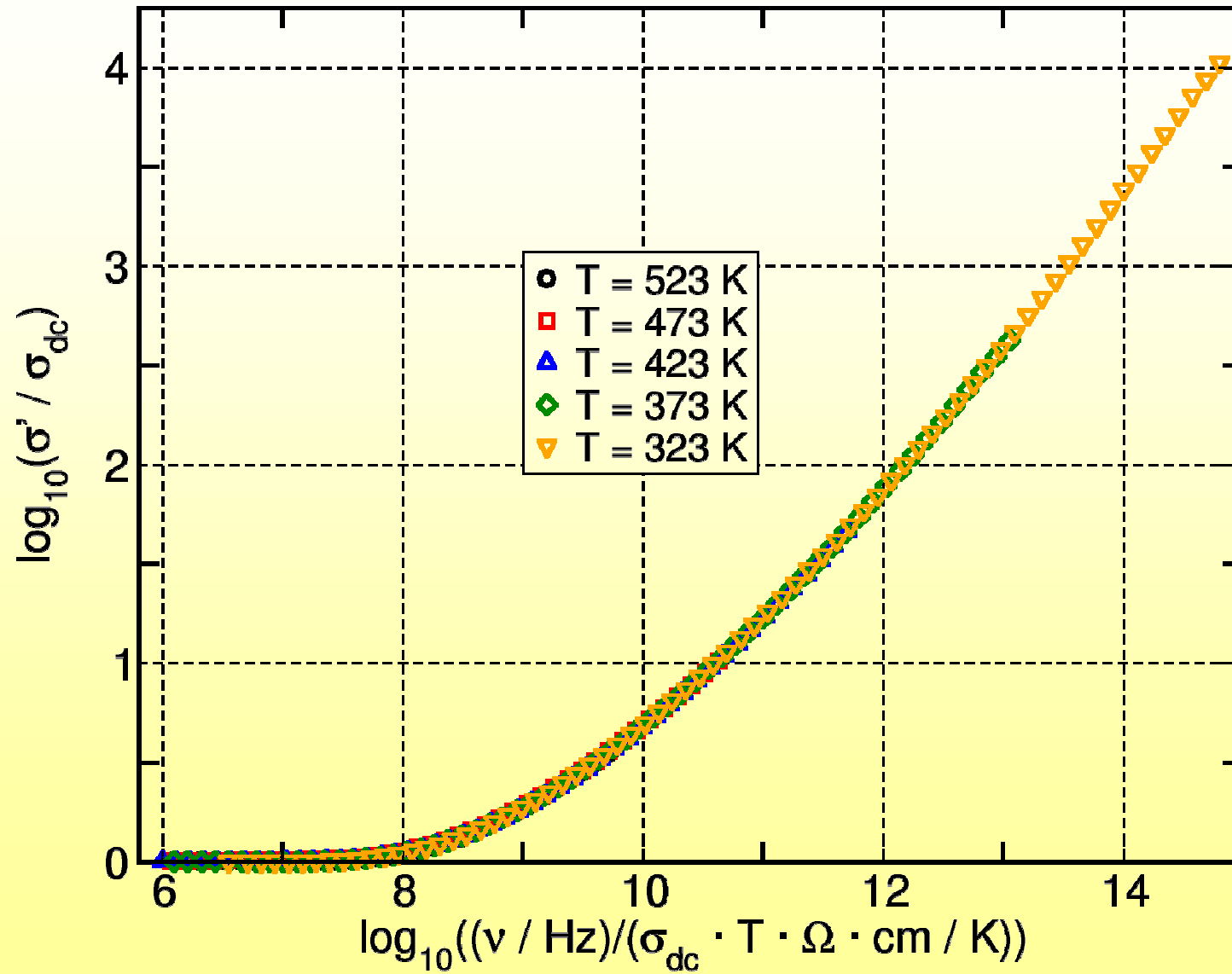
Quasi-universal shape of conductivity spectra  
(virtually independent of composition)

Is there a quasi-universal ion transport mechanism?

# Conductivity spectra of a 0.213 Na<sub>2</sub>O \* 0.787 GeO<sub>2</sub> glass

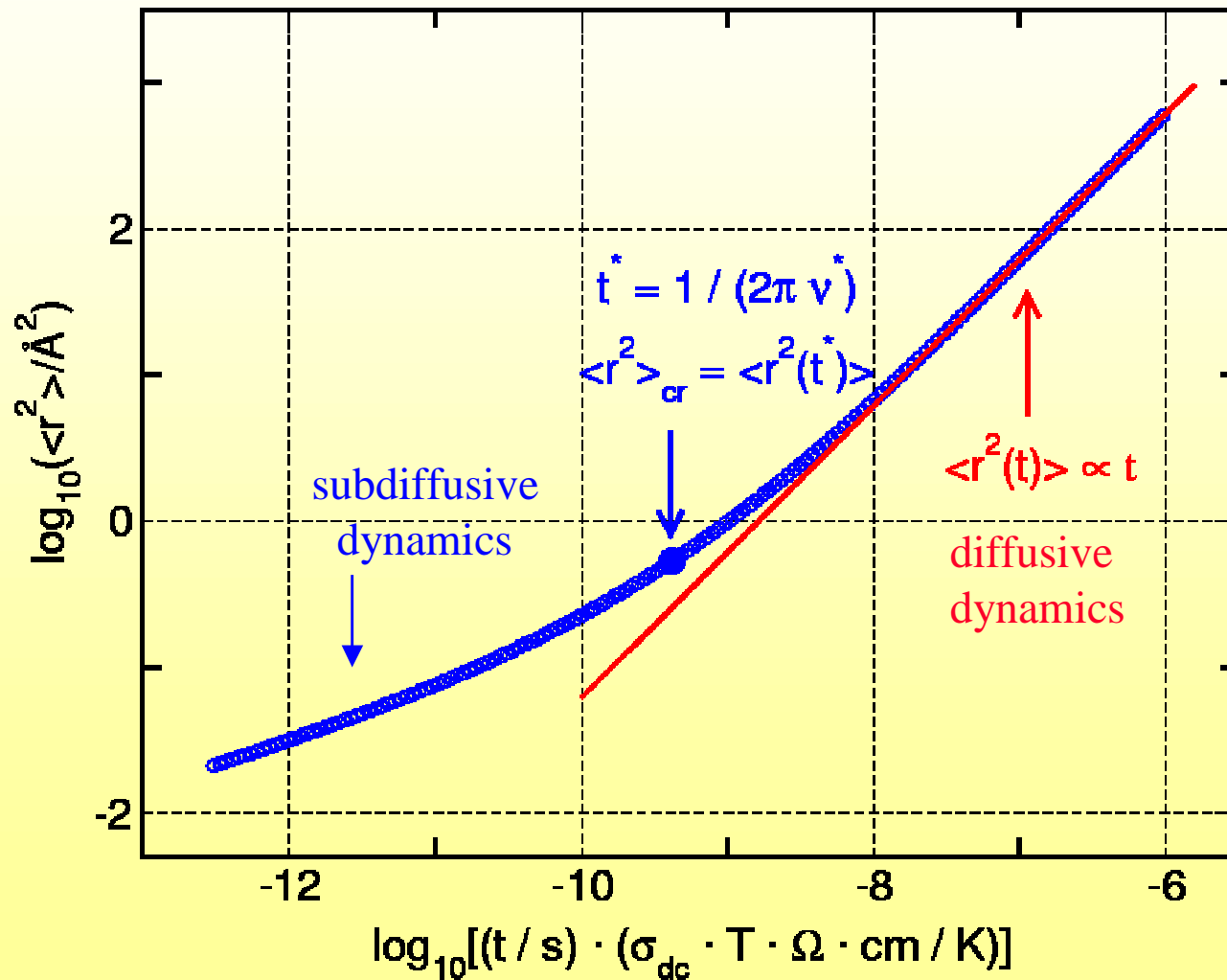


# Summerfield scaling

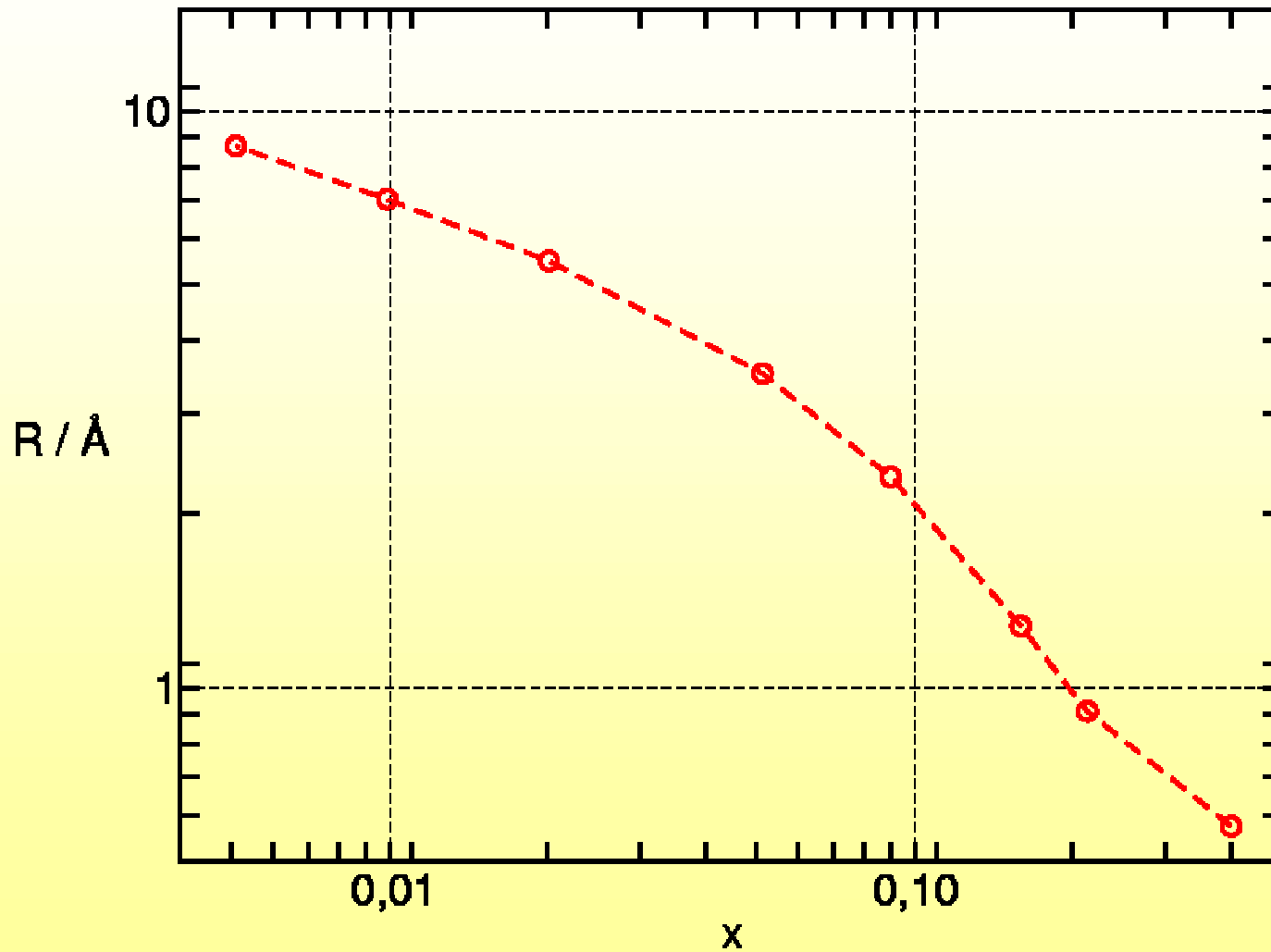


# Master curve of the time-dependent mean square displacement of the mobile $\text{Na}^+$ ions, $\langle r^2(t) \rangle$

0.213  $\text{Na}_2\text{O}$  \* 0.787  $\text{GeO}_2$  glass



*Spatial extent of subdiffusive ion dynamics*  $R \equiv \sqrt{\langle r^2 \rangle_{cr}}$   
for  $x \text{ Na}_2\text{O} * (1 - x) \text{ GeO}_2$  glasses



B. Roling, C. Martiny, S. Brückner, *Phys. Rev. B* **63** (2001) 214203.

Assumption: Typical hopping distance of Na<sup>+</sup> ions:  $d \approx 3 \text{ \AA}$ <sup>o</sup>  
(Molecular dynamics simulations)

Glass with  $x = 0.005$ :  $\langle r^2 \rangle_{cr} > d^2$

→ At the crossover time  $t^*$ , the ions have moved, on the average, over *several hopping distances*.

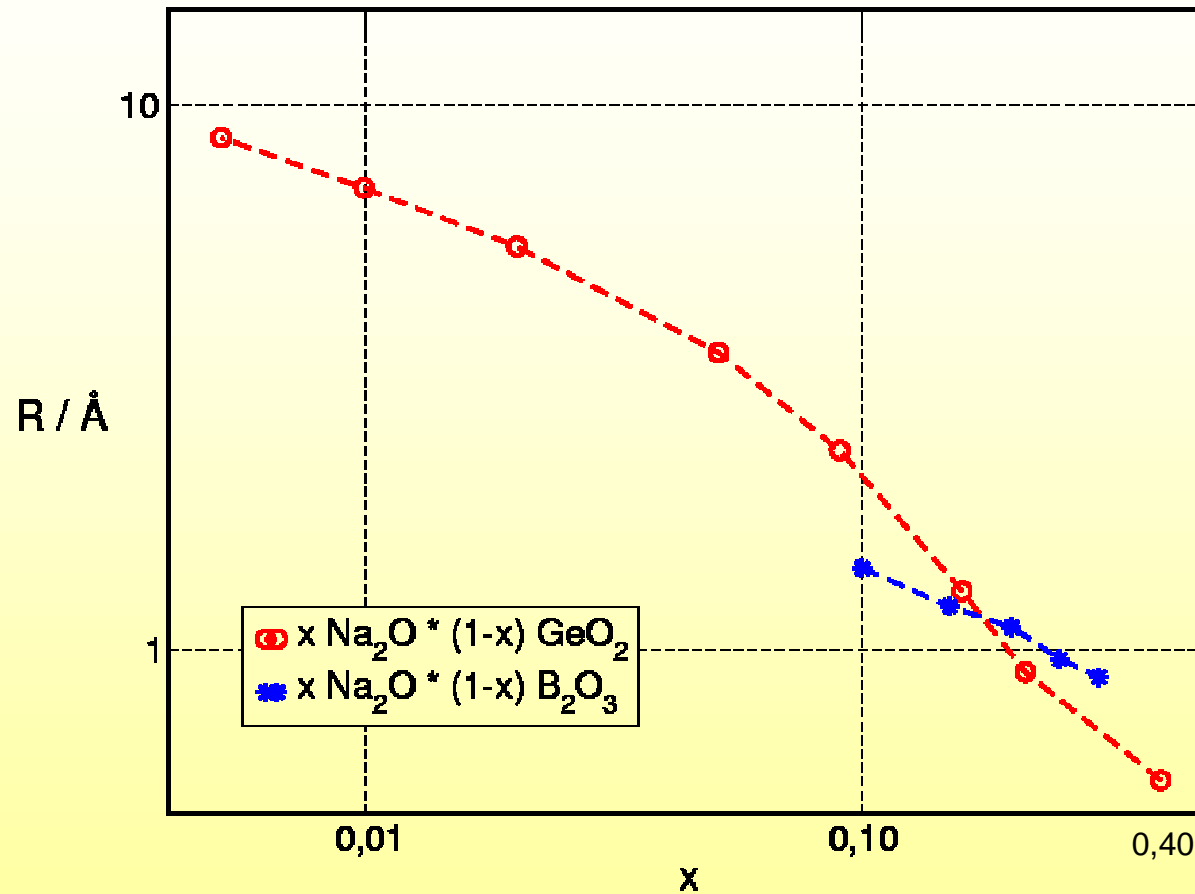
Glass with  $x = 0.40$ :  $\langle r^2 \rangle_{cr} < d^2$

→ At the crossover time  $t^*$ , only a *small fraction of ions* have left their original sites.



Despite the quasi-universal shape of the conductivity spectra, the microscopic mechanisms of the ion transport depend on glass composition.

*Spatial extent of subdiffusive ion dynamics R*  
for  $x \text{ Na}_2\text{O} * (1 - x) \text{ GeO}_2$  and  $x \text{ Na}_2\text{O} * (1 - x) \text{ B}_2\text{O}_3$  glasses

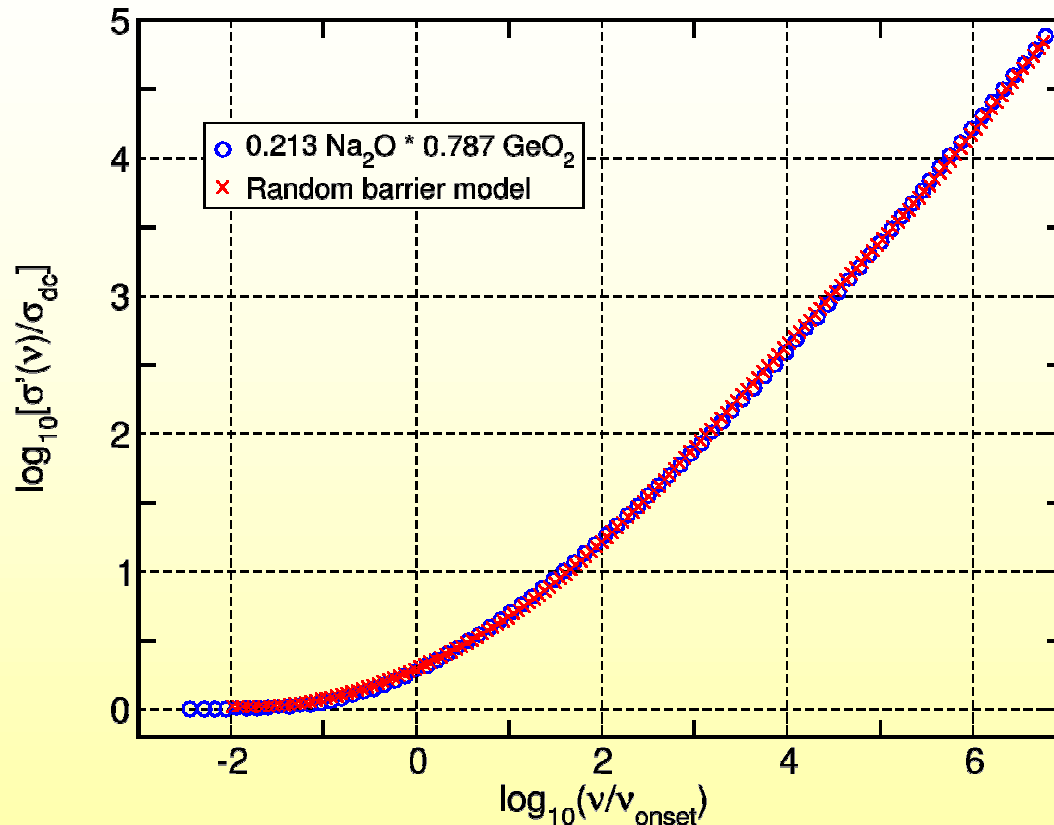


B. Roling, C. Martiny,  
S. Brückner,  
*Phys. Rev. B*  
**63** (2001) 214203.

→  $R$  depends on *structure of the glass network*.



## Comparison with Random Barrier Model



B. Roling,  
*Phys. Chem.  
 Chem. Phys.*  
**3** (2001) 5093.

See also:  
 J. C. Dyre, T. Schroeder,  
*Rev. Mod. Phys.*  
**72** (2000) 873.

However: Random Barrier Model:  $\langle r^2 \rangle_{cr} \propto T^{-1.3}$  (Number of continuous conduction pathways depends on temperature.)

Most ion conducting glasses:  $\langle r^2 \rangle_{cr}$  independent of T

## Almond and West formalism

- Determine crossover frequency  $\nu^*$

- Take random walk expression: 
$$\sigma_{dc} = \frac{N_{V,\text{mobile ions}} \cdot q^2 \cdot a^2 \cdot \Gamma}{6 \cdot k_b \cdot T}$$

and identify crossover frequency  $\nu^*$  with hopping rate  $\Gamma$

- Assumption for hopping distance:  $a = 2.5 - 3 \text{ \AA}$

➔ Number density of mobile ions  $N_{V,\text{mobile ions}}$

**Problem: Random walk expression is not valid!**

In a first approximation: 
$$\frac{N_{V,\text{mobile ions}}}{N_{V,\text{all ions}}} \approx \frac{\langle r^2 \rangle_{cr}}{a^2}$$

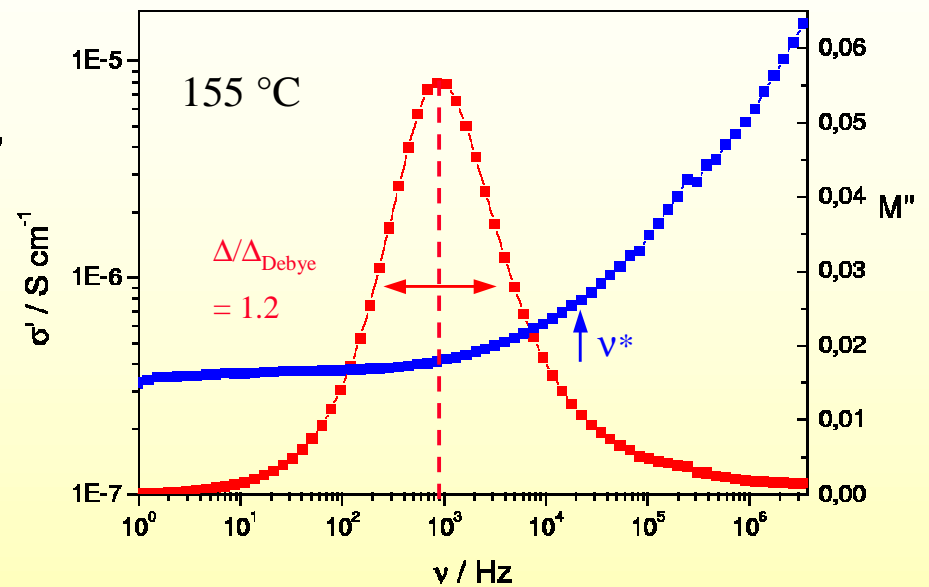
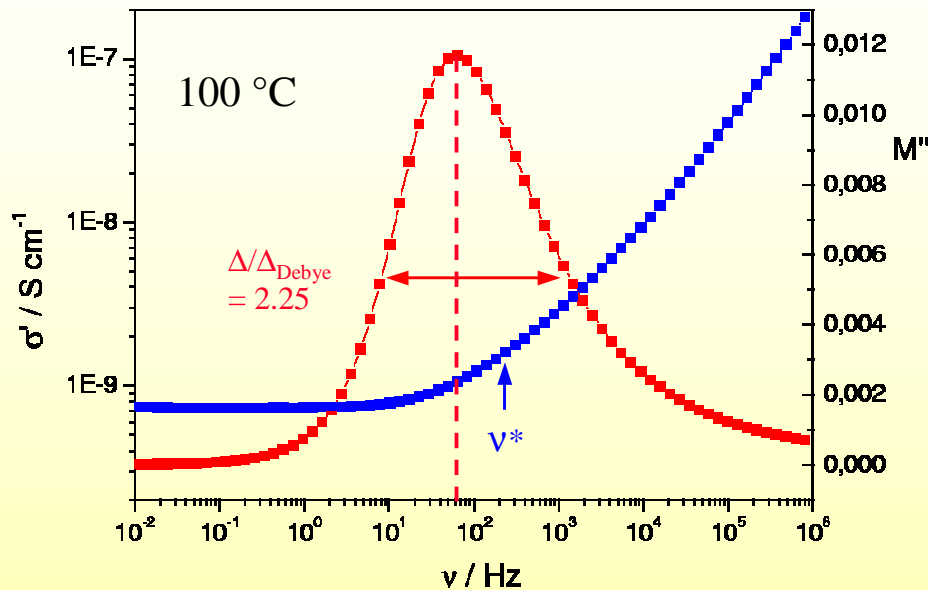
➔ Number of ions that have moved at the crossover time  $t^*$   
(**Not** number of ions that contribute to dc conductivity!)

# Modulus formalism

$$\hat{M} = \frac{1}{\hat{\epsilon}} = \frac{i \cdot \omega \cdot \epsilon_0}{\hat{\sigma}}$$

0.20 Na<sub>2</sub>O \* 0.80 GeO<sub>2</sub>

0.0005 K<sub>2</sub>S \* 0.9995 B<sub>2</sub>S<sub>3</sub>



$$\frac{\nu_{M'' \text{ peak}}}{\nu^*} \approx \frac{\Delta \epsilon}{\epsilon'(\infty)}$$

Dielectric relaxation strength due to subdiffusive ion dynamics

Vibrational and electronic polarisation

With decreasing mobile ion concentration,  $\Delta\epsilon$  decreases and the modulus peak shifts into the dc conductivity regime.

## **Misinterpretation of modulus peak narrowing with decreasing ion concentration:**

With decreasing ion concentration, the ionic movements become less correlated.

## **Correct interpretation of conductivity spectra using linear response theory:**

With decreasing ion concentration, the spatial extent of the subdiffusive ion dynamics (of the correlated forward-backward movements) increases!

## 2. Nonlinear (High-Field) Conductivity Spectroscopy

**Example:** Solid electrolyte sample with thickness  $d = 100 \text{ nm}$

Applied voltage  $U = 5 \text{ V}$

→ Electric field strength  $E = 500 \text{ kV / cm}$

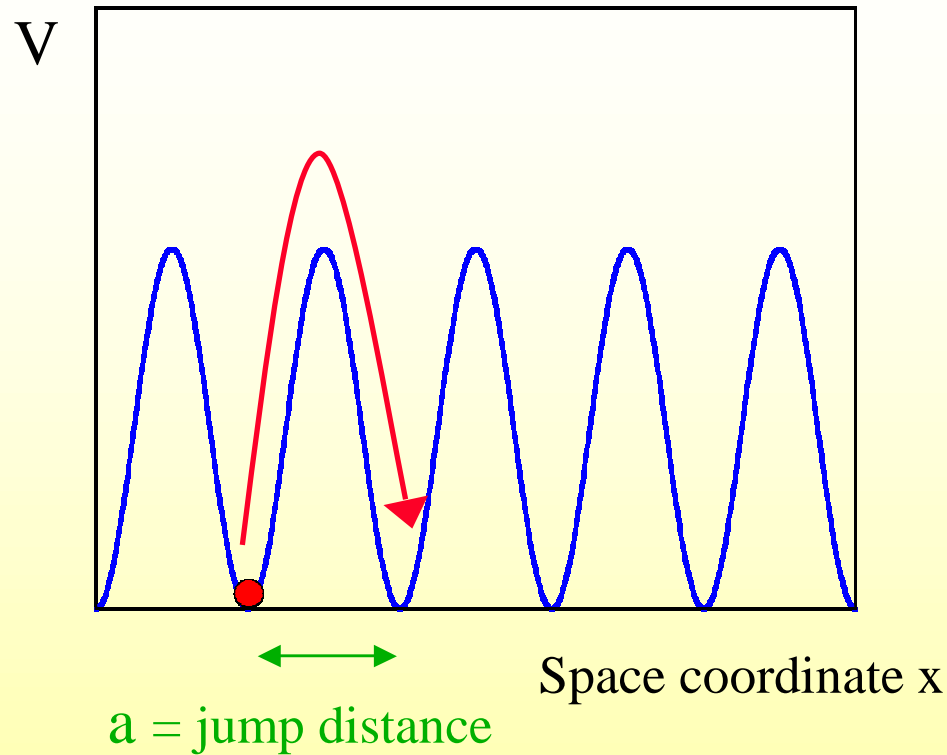
At field strengths  $E > 50 \text{ kV/cm}$ , the ionic conductivity of many solid electrolytes becomes field-dependent.

Current density  $j = \sigma_1 \cdot E + \sigma_3 \cdot E^3 + \sigma_5 \cdot E^5 + \dots$

↑  
Low-field  
conductivity

↑  
Higher-order  
conductivity coefficients

## 'Random walk' in a periodic potential landscape



Current density

$$j \propto \sinh\left(\frac{qaE}{2kT}\right)$$

$q$  = charge of particle

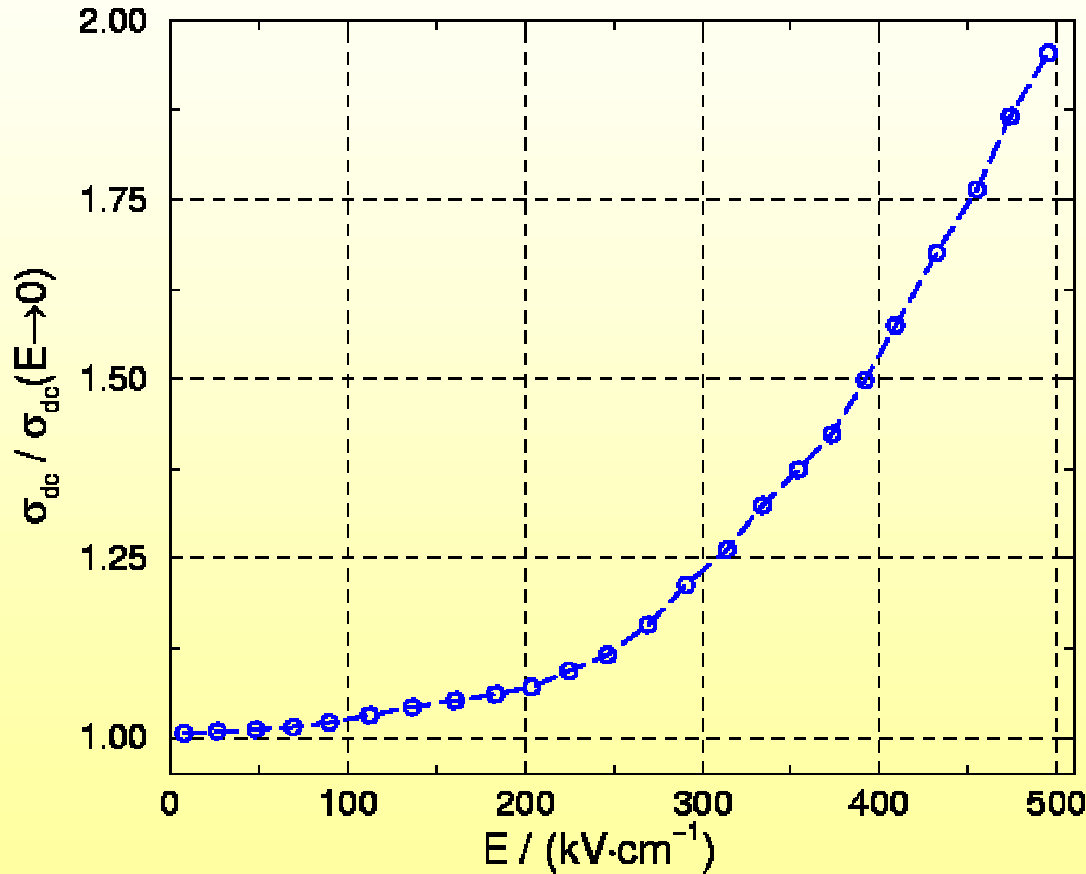
$k$  = Boltzmann's constant

$T$  = temperature

Field dependence of current density provides *direct information* about jump distance  $a$ .

# Field dependence of the dc conductivity of solid electrolytes

**Thuringian glass:** 0.101 Na<sub>2</sub>O \* 0.084 CaO \* 0.030 Al<sub>2</sub>O<sub>3</sub> \* 0.785 SiO<sub>2</sub>



Fit with

$$j \propto \sinh\left(\frac{qa_{app}E}{2kT}\right)$$



Apparent  
jump distance

$$a_{app} = 15 \overset{\circ}{\text{Å}} \dots 30 \overset{\circ}{\text{Å}}$$

(found for various glasses)

J. M. Hyde et al., Phys. Chem. Glasses 27 (1986) 147.

## Previous studies: DC electric fields

- No direct information on Joule heating  
(Joule heating may pretend nonlinear ion transport.)
- Only one relation:  $\sigma_{dc}(E_{dc})$

## Our method: AC electric fields

- Unambiguous differentiation between nonlinear ion transport and Joule heating
- $\sigma_1(v)$ ,  $\sigma_3(v)$ ,  $\sigma_5(v)$ , ....  
    **➔** More information



## Glasses studied:

- 0.127 Na<sub>2</sub>O \* 0.096 CaO \* 0.062 Al<sub>2</sub>O<sub>3</sub> \* 0.715 SiO<sub>2</sub> (NCAS12)

[ Composition similar to Thuringian glass:  $a_{\text{app}} = 15.5 \text{ \AA}$  (from sinh fit) ]

- 0.25 Na<sub>2</sub>O \* 0.096 CaO \* 0.062 Al<sub>2</sub>O<sub>3</sub> \* 0.592 SiO<sub>2</sub> (NCAS25)
- 

- 0.20 Na<sub>2</sub>O \* 0.80 SiO<sub>2</sub>

- 0.25 Na<sub>2</sub>O \* 0.75 SiO<sub>2</sub>

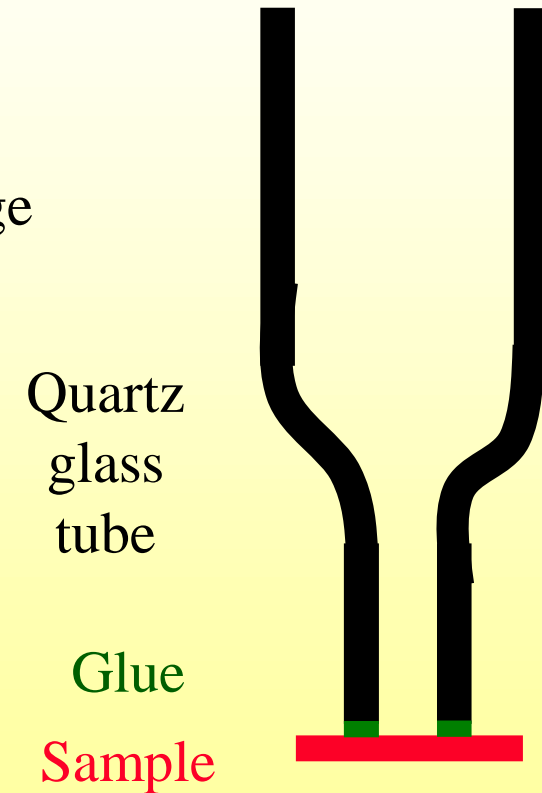
## Preparation of thin glass samples

- High-precision cutting and grinding of bulk glass samples:

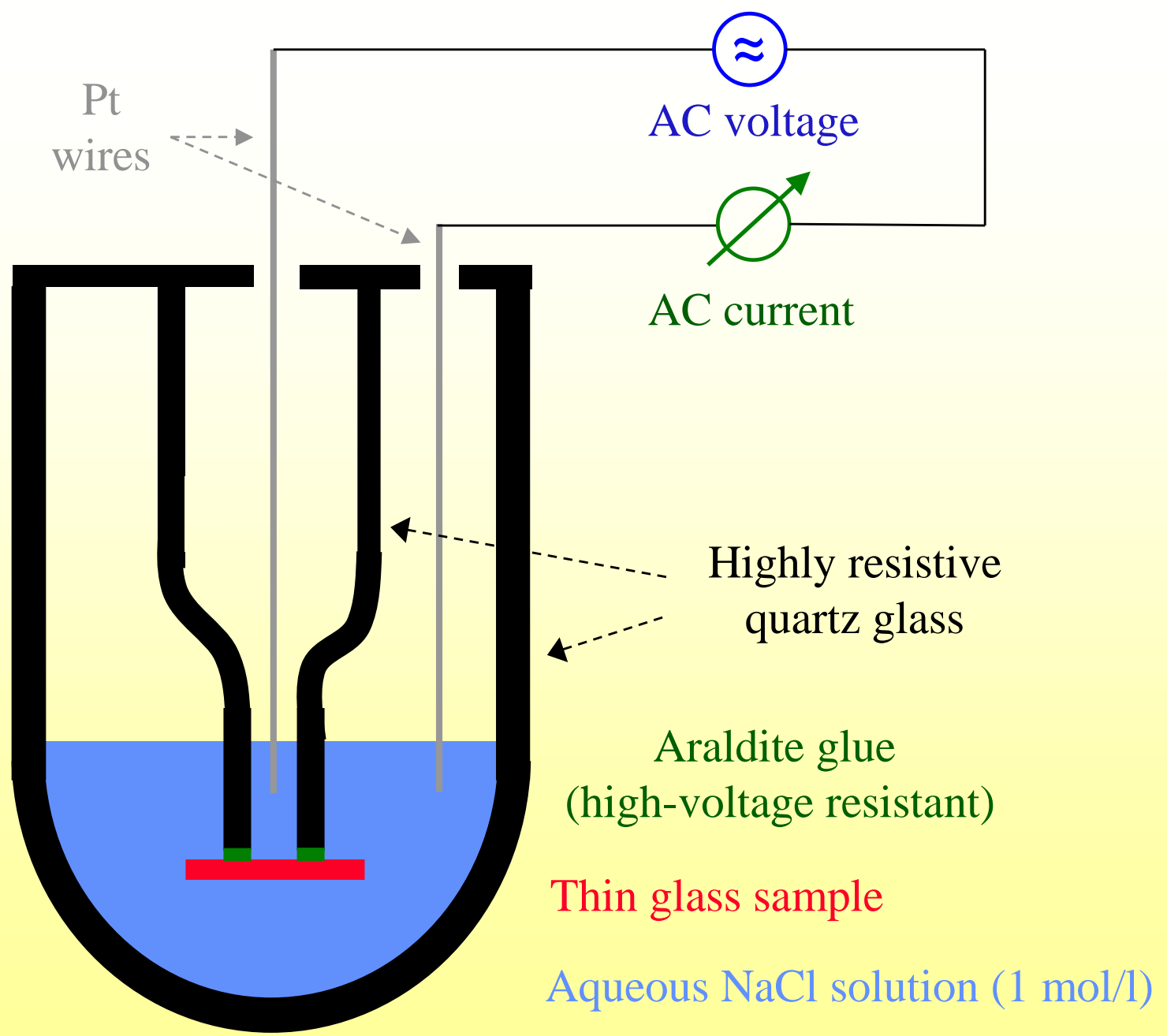
→ Sample thickness: 60 – 100  $\mu\text{m}$

- Samples are attached to high-resistance quartz glass tube ( $\sigma < 10^{-16}$  S/cm) by using a high-voltage resistant araldite glue.

- Chemical etching with HF: 40 - 50  $\mu\text{m}$



→ Electric fields of 100 - 125 kV /cm at  $U = 500$  V



Pt  
wires

AC voltage

AC current

Highly resistive  
quartz glass

Araldite glue  
(high-voltage resistant)

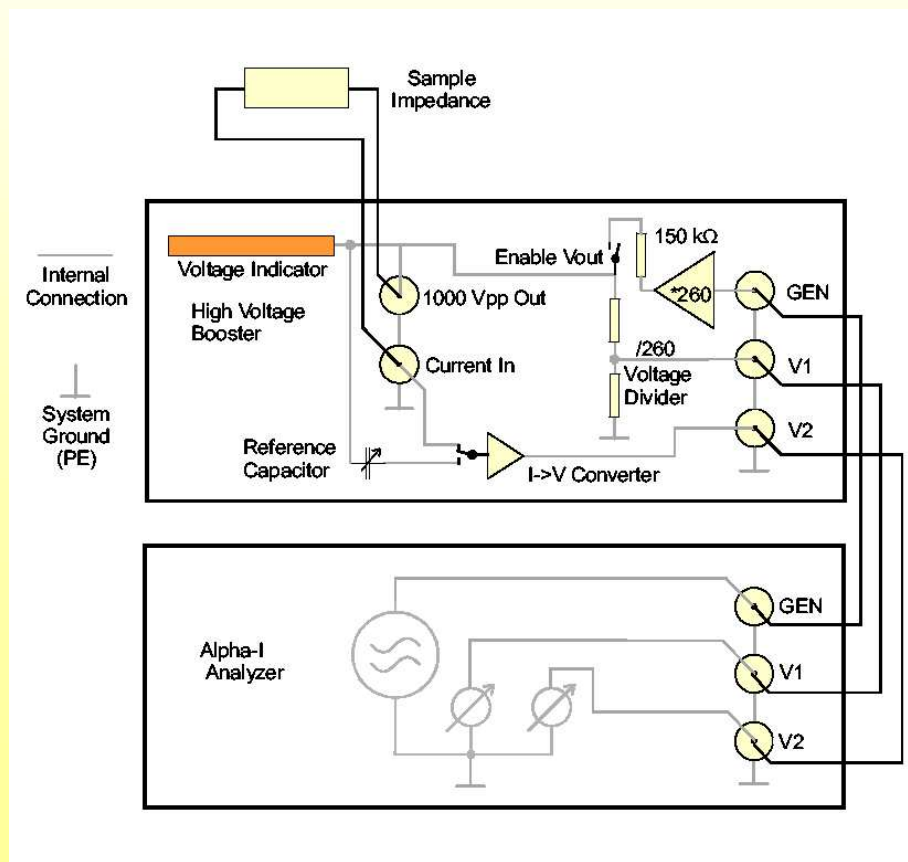
Thin glass sample

Aqueous NaCl solution (1 mol/l)

## High-voltage measurement system

Novocontrol  $\alpha$ -S High Resolution Dielectric Analyser, equipped with:

- Broadband High-Voltage Amplifier,
- Broadband Dielectric Converter



Frequency range:  $< 10$  kHz

Maximum amplitude of  
ac voltage: 500 V

Detection of **higher harmonics**  
in current spectra

## Analysis of nonlinear ion transport by means of higher harmonics

**Example:** Electrical properties of ion conducting sample are given by:

$$j = \sigma_1 \cdot E + \sigma_3 \cdot E^3$$

Electric field  $E = E_0 \cdot \sin(\omega t)$

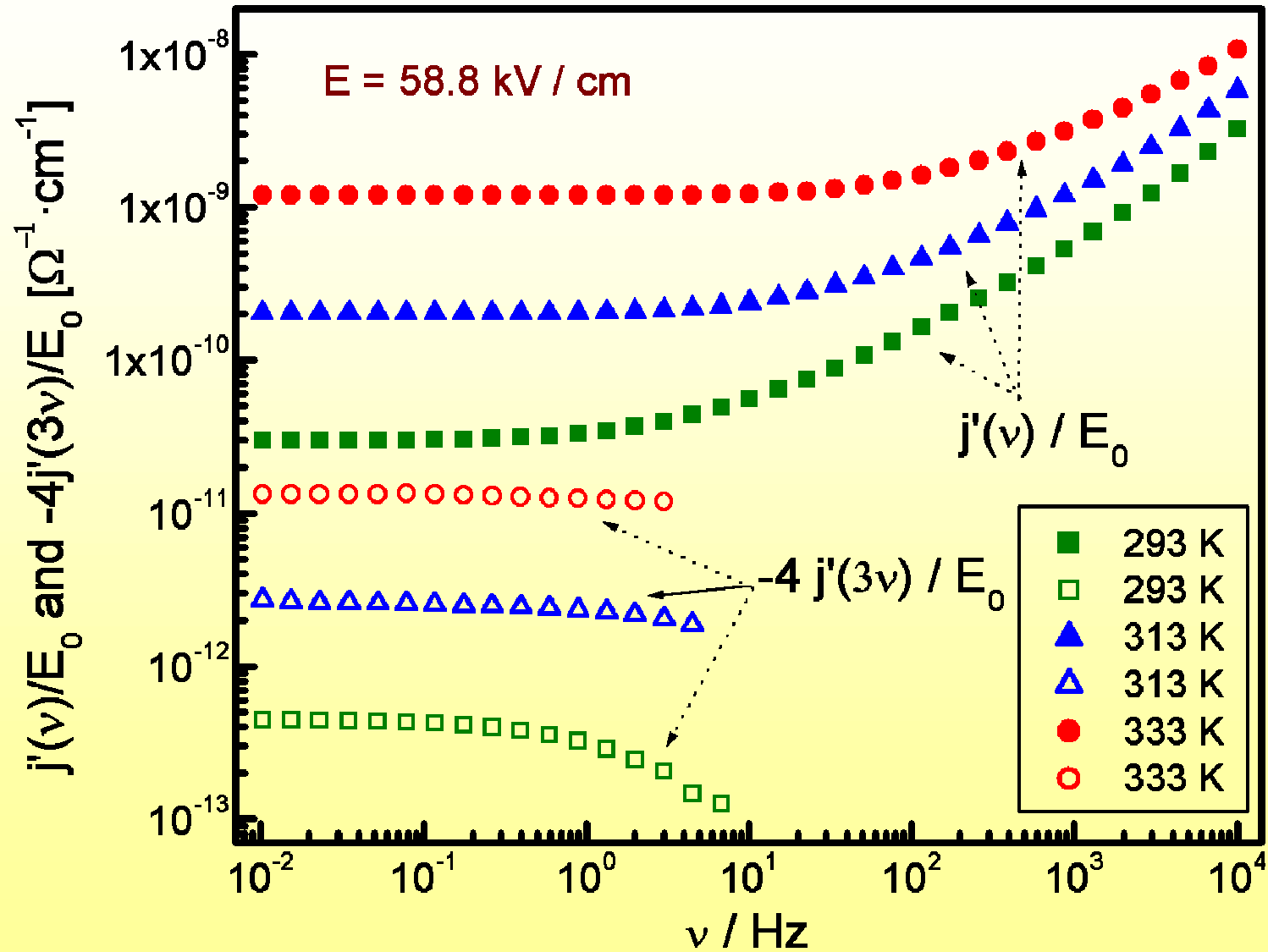


$$j = \sigma_1 \cdot E_0 \cdot \sin(\omega t) + \sigma_3 \cdot (E_0)^3 \cdot \sin^3(\omega t)$$

$$= \sigma_1(\omega) \cdot E_0 \cdot \sin(\omega t) + \frac{3}{4} \sigma_3(\omega) \cdot (E_0)^3 \cdot \sin(\omega t) - \underbrace{\frac{1}{4} \sigma_3(3\omega) \cdot (E_0)^3 \cdot \sin(3\omega t)}_{\text{Harmonic at } 3\omega}$$

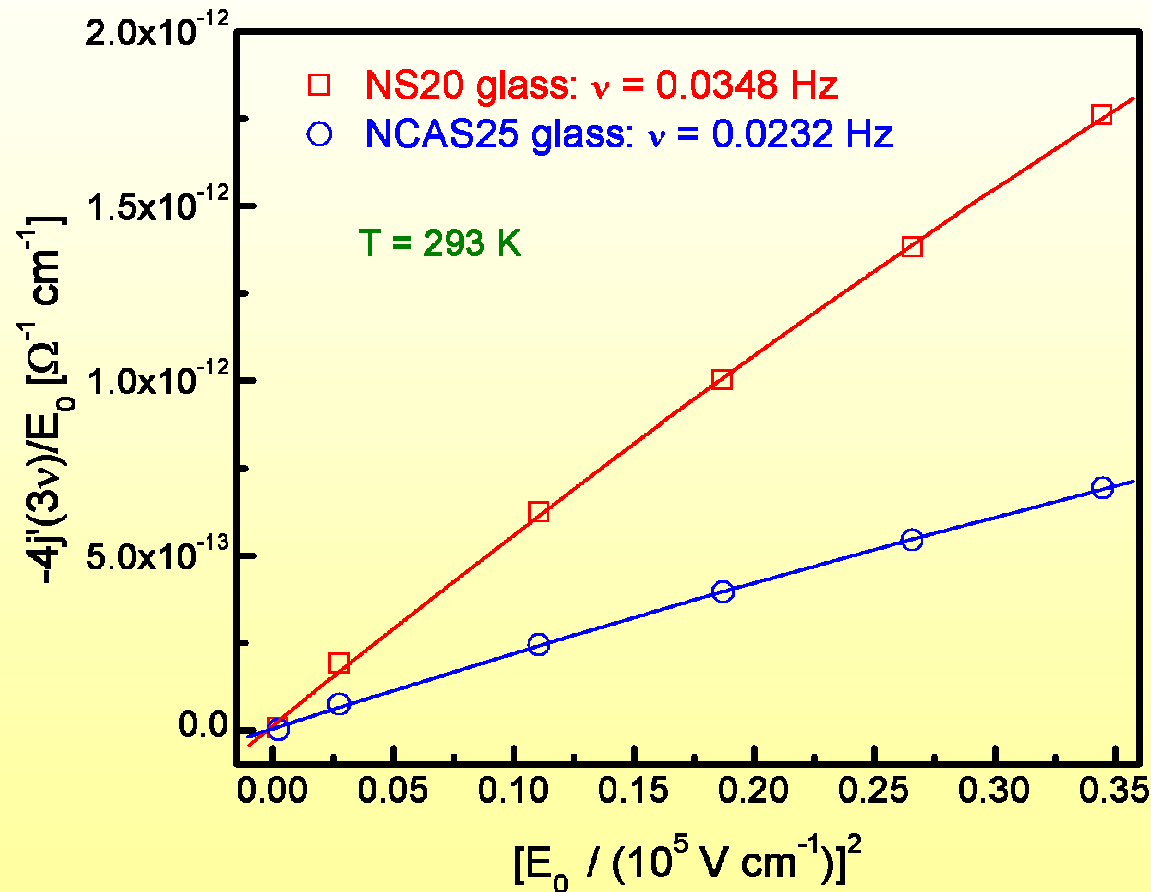
Unambiguous differentiation between nonlinear ion transport and Joule heating.

# Results for 0.2 Na<sub>2</sub>O \* 0.8 SiO<sub>2</sub> glass (NS20)



## Determination of higher-order conductivity coefficients

$$\frac{-4 \cdot j'(3\nu)}{E_0} = \sigma'_3(3\nu) \cdot (E_0)^2 + \frac{5}{4} \cdot \sigma'_5(3\nu) \cdot (E_0)^4 + \dots$$



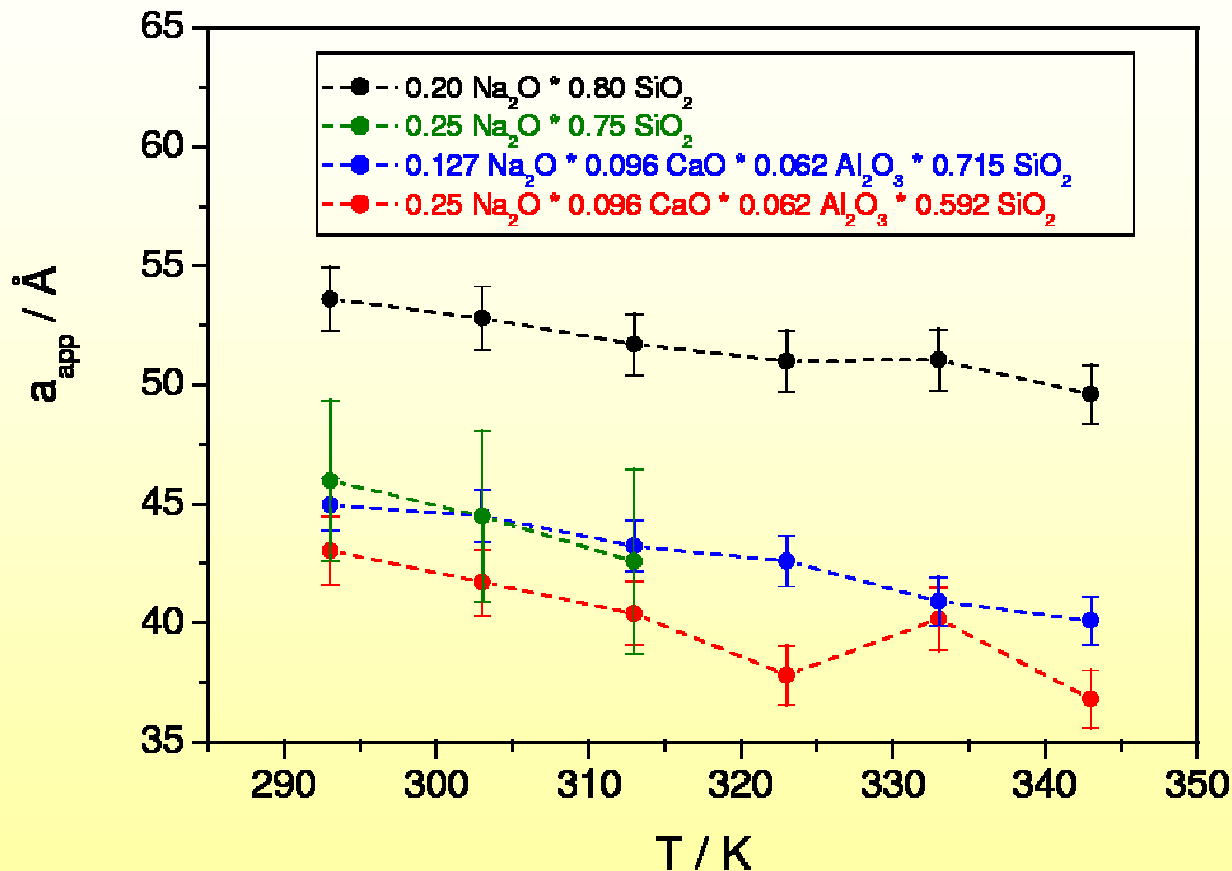
Fit by second-order polynomial

- Linear term:  $\sigma_{3,\text{dc}}$
- Negative quadratic term:  $\sigma_{5,\text{dc}} < 0$

## Apparent jump distances

$$a_{\text{app}} = \sqrt{\frac{\sigma_{3,\text{dc}} \cdot 24 \cdot (kT)^2}{\sigma_{1,\text{dc}} \cdot q^2}}$$

(Taylor expansion of sinh function)



Taylor expansion of sinh function:

$$\sigma_{5,\text{dc}} > 0$$



Experiment:

$$\sigma_{5,\text{dc}} < 0$$

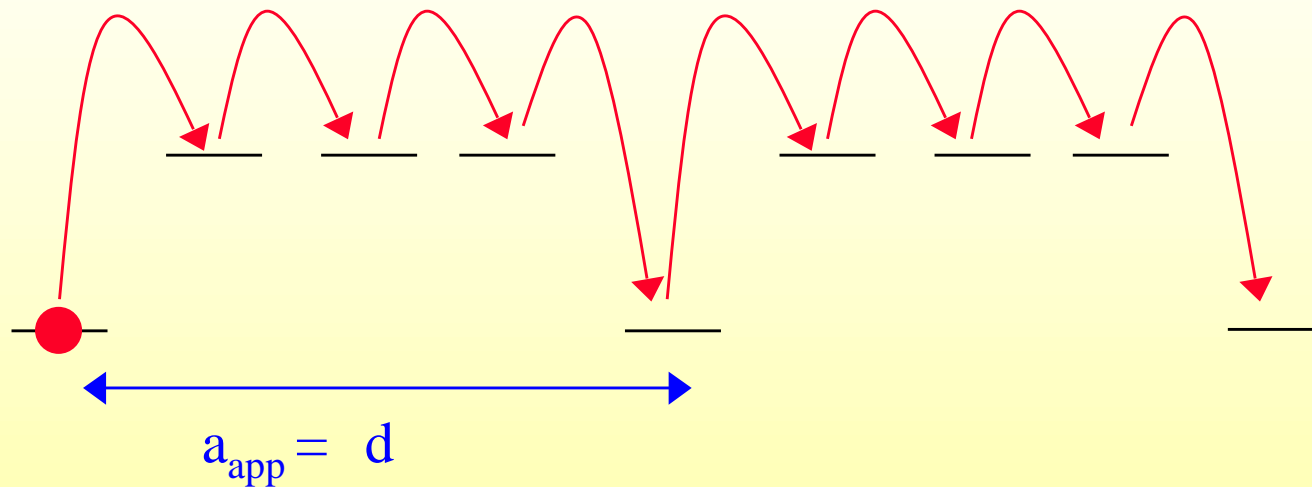
- Values are larger than literature values from dc measurements.
- $a_{\text{app}}$  decreases with increasing temperature  $T$ .
- $a_{\text{app}}$  decreases with increasing  $\text{Na}_2\text{O}$  content.



## What is the physical meaning of the apparent jump distance?

(Collaboration with Prof. Andreas Heuer, Institute of Physical Chemistry, and Prof. Rudolf Friedrich, Institute of Theoretical Physics, Münster)

### One-dimensional periodic potential landscape:



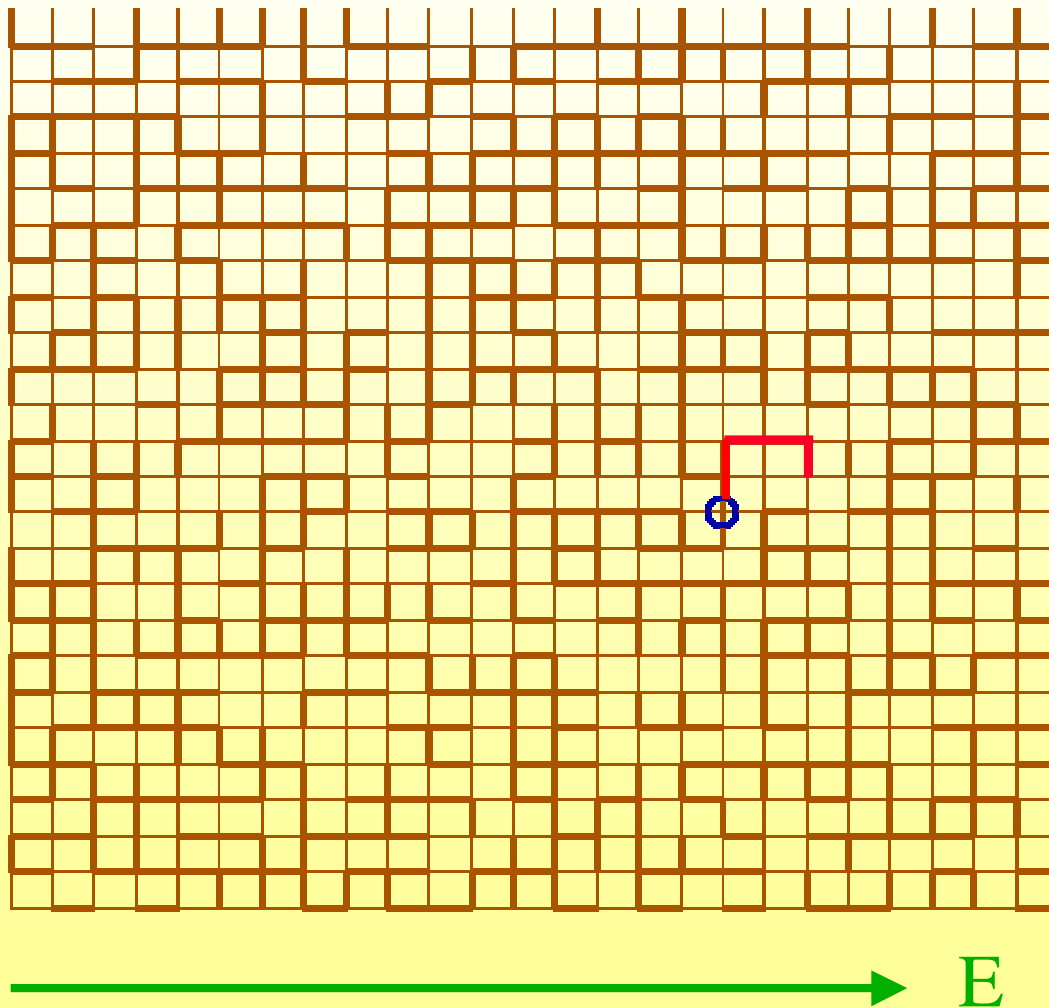
→ Is the apparent jump distance related to the distance between **low-energy sites** in an ionic conductor?

However: Things become more complicated in **two- and three-dimensional disordered potential landscapes.**

# Nonlinear conductivity of particles in a random barrier landscape

Monte Carlo simulations:  $\sigma_{3,dc}$  is negative!

B. Roling, *J. Chem. Phys.*  
117 (2002) 1320.



Field-induced  
trapping of particles  
in dead ends

## Summary and Outlook

- Apparent jump distance  $a_{\text{app}}$  decreases with increasing temperature and increasing sodium oxide content.
- The fifth-order coefficient  $\sigma_{5,\text{dc}}$  is negative (for all glasses and at all temperatures).
- Random Barrier Model predicts negative values for  $\sigma_{3,\text{dc}}$ . Experimental values for  $\sigma_{3,\text{dc}}$  are positive.
- Further theoretical studies on nonlinear ion transport in disordered potential landscapes
  - ➔ Deeper understanding of physical meaning of large apparent jump distances and of negative values for  $\sigma_{5,\text{dc}}$

### 3. Electrostatic force spectroscopy (Nanoscale conductivity spectroscopy)

Established methods for characterising ion dynamics and transport in solid electrolytes:

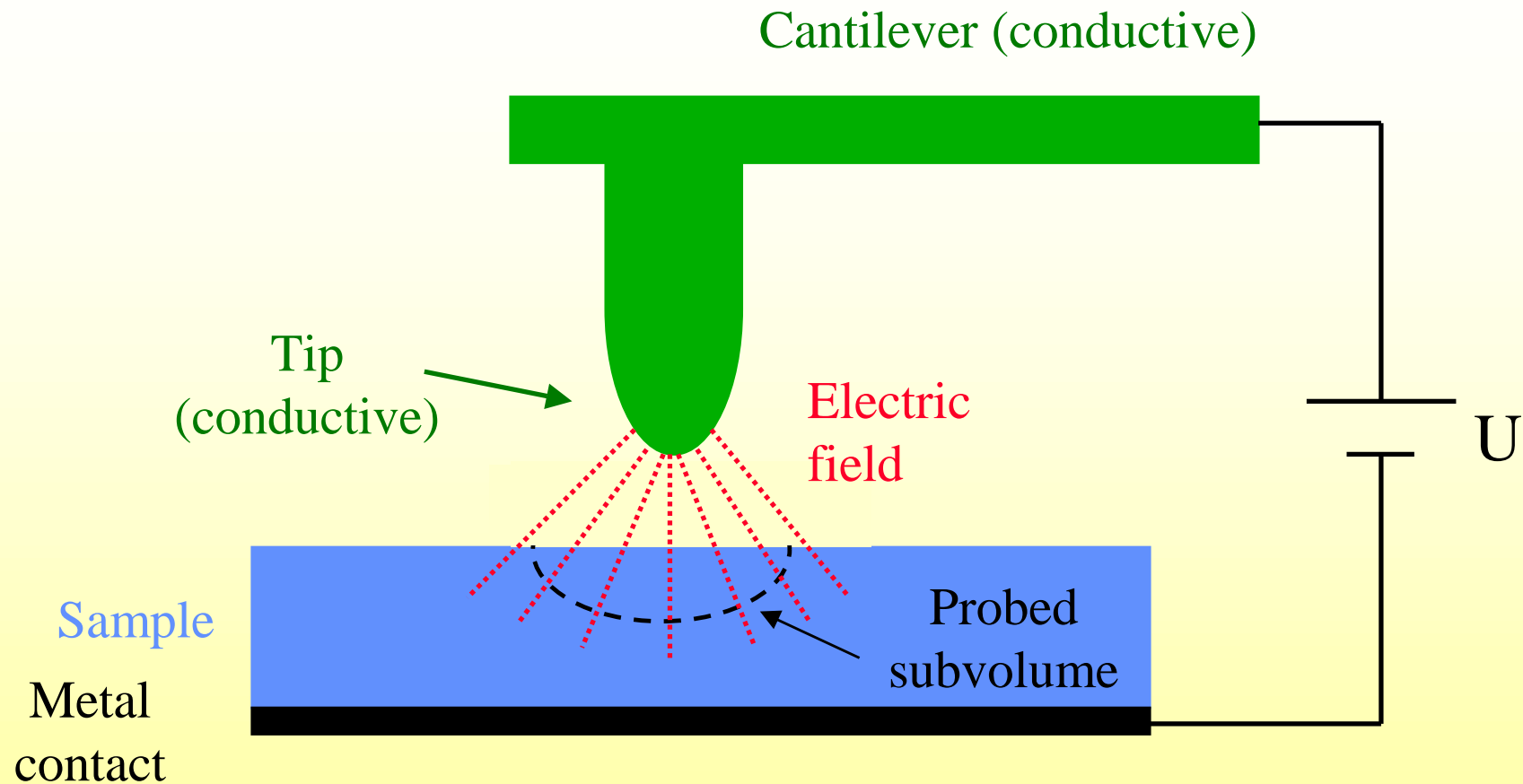
- Macroscopic conductivity spectroscopy
- Quasielastic neutron scattering
- Mechanical relaxation spectroscopy
- NMR relaxation techniques

Macroscopic averaging over the dynamics of more than  $10^{20}$  mobile ions.

→ Loss of information about microscopic mechanisms

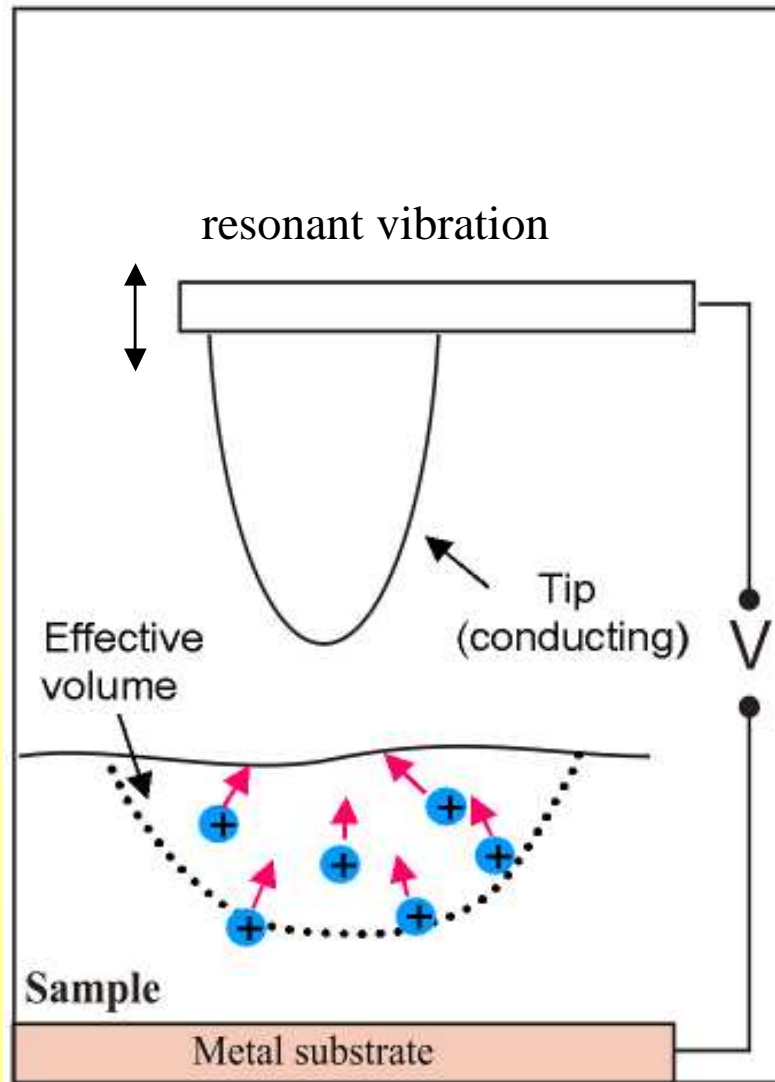
High loss of information in nano- and mesostructured materials:  
Ion dynamics and transport in different phases and at interfaces.

# Electrical force microscopy



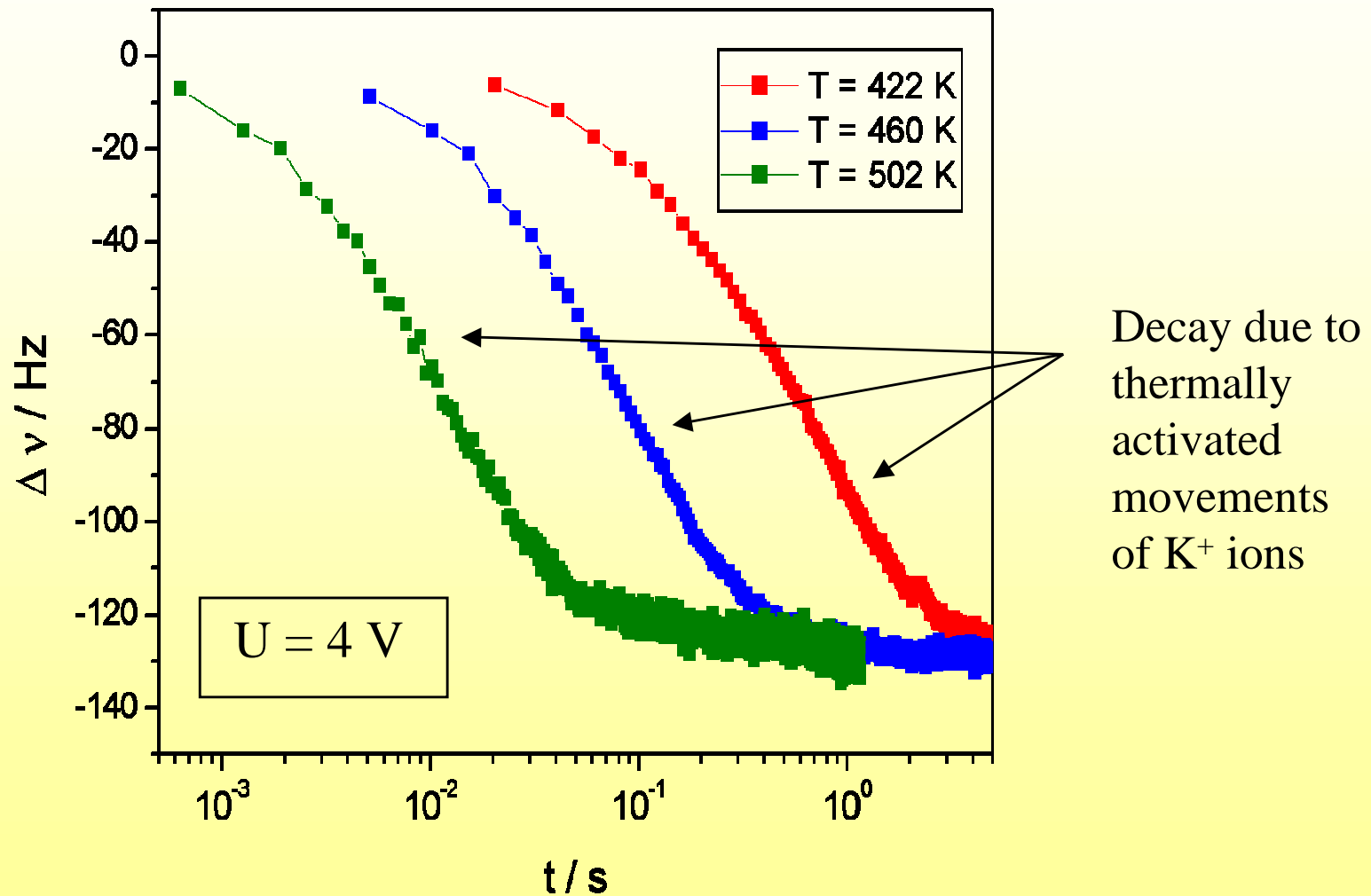
A large part of the voltage drop in the sample occurs in a small subvolume of the order  $(\text{tip diameter})^3$ .

## Electrostatic force spectroscopy



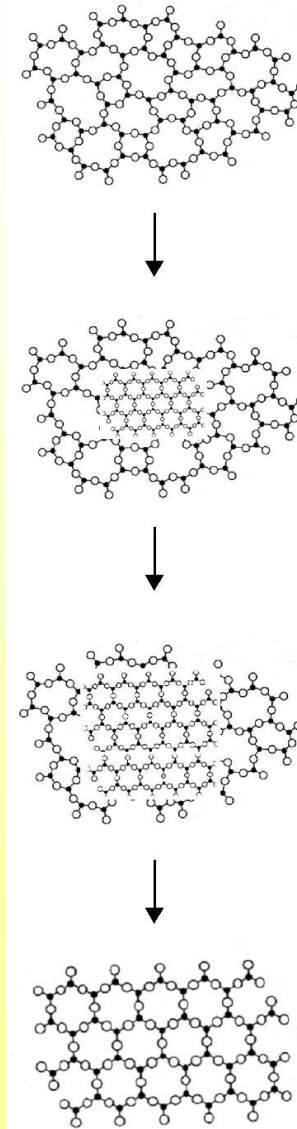
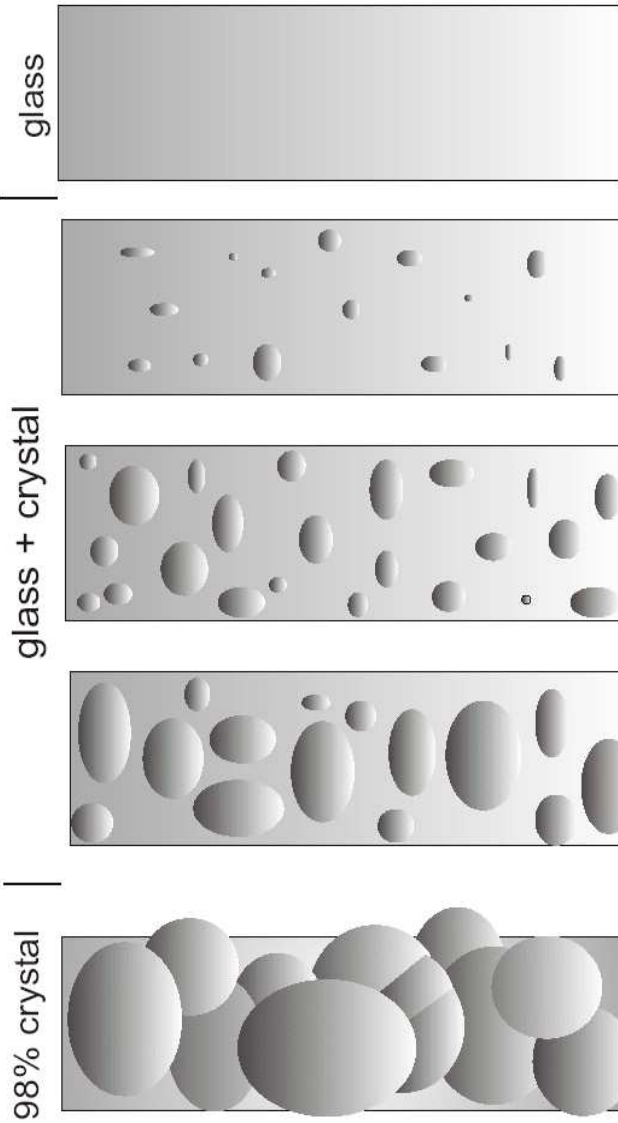
- Mobile ions move into field direction.
- Changes in the electrical forces between tip and sample.
- Changes in the resonant frequency of the cantilever.
- The ionic movements generate a counter field that impedes further ionic movements.
- The resonant frequency of the cantilever becomes constant.

Time dependence of the cantilever resonant frequency  
for a  $\text{K}_2\text{O} * 2 \text{CaO} * 4 \text{SiO}_2$  glass



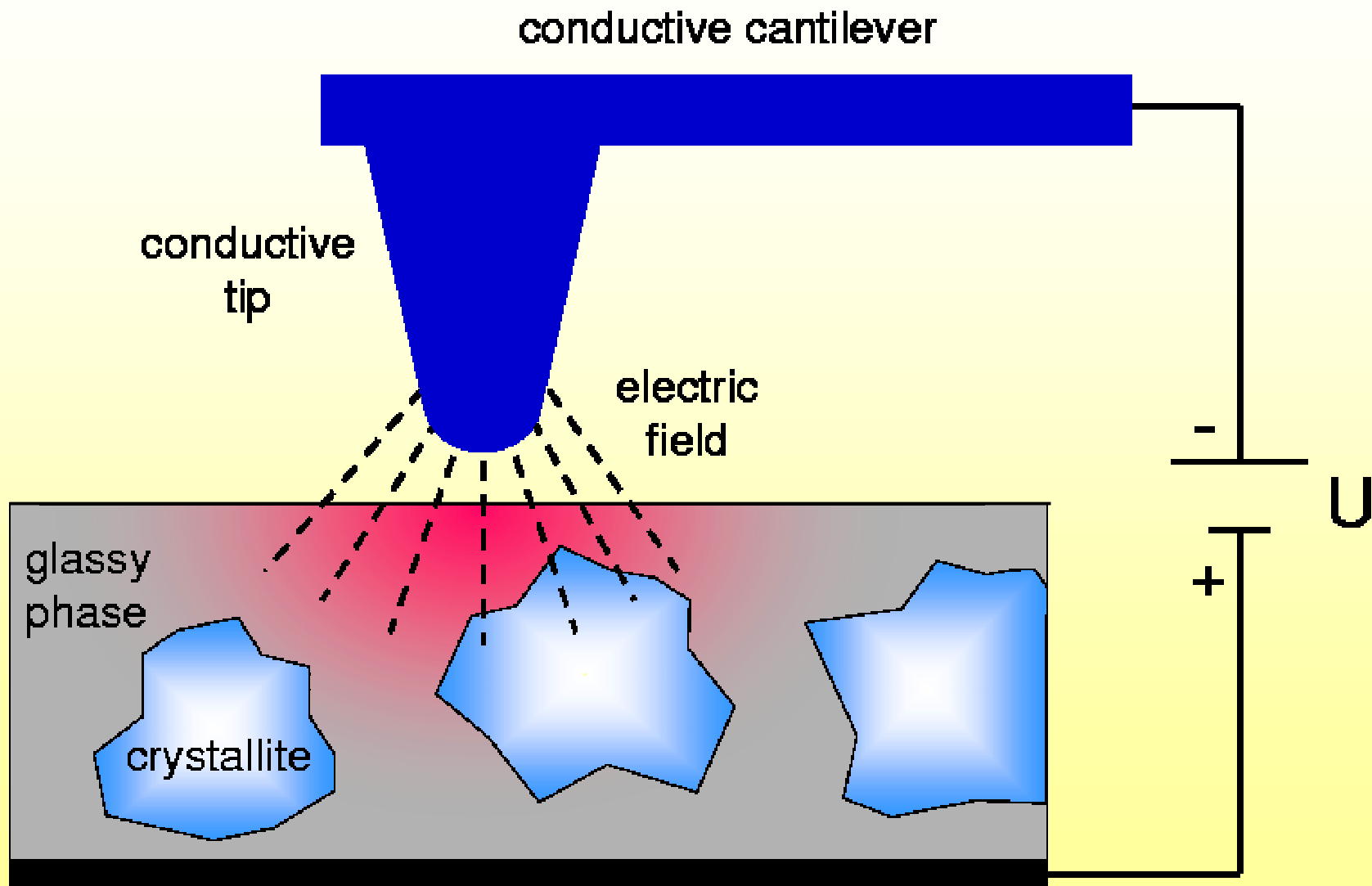
# Spatially resolved spectroscopy on glass ceramics

Increasing  
annealing temperature  
and/or  
annealing time



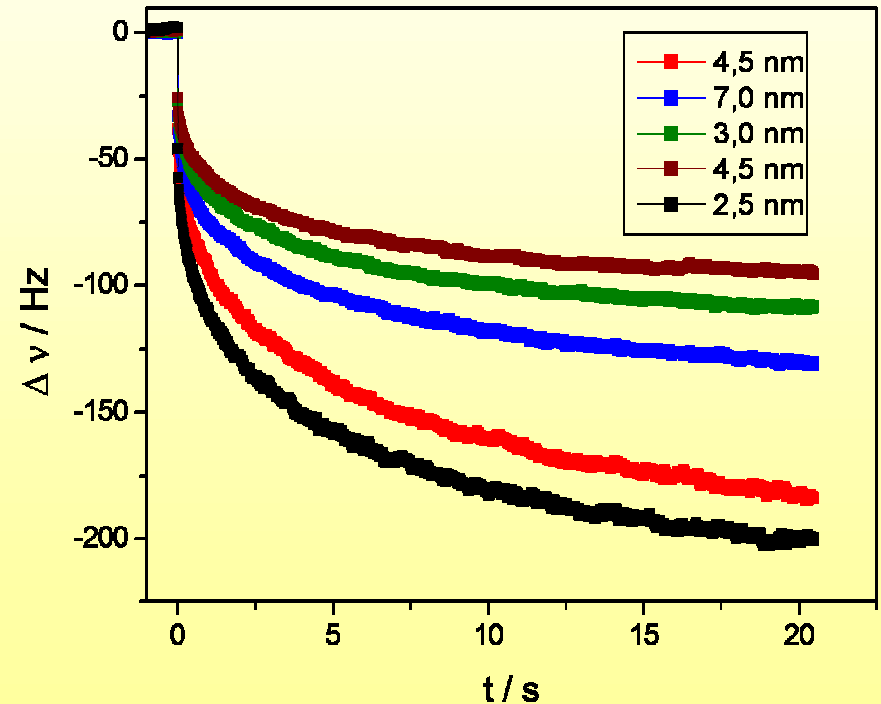
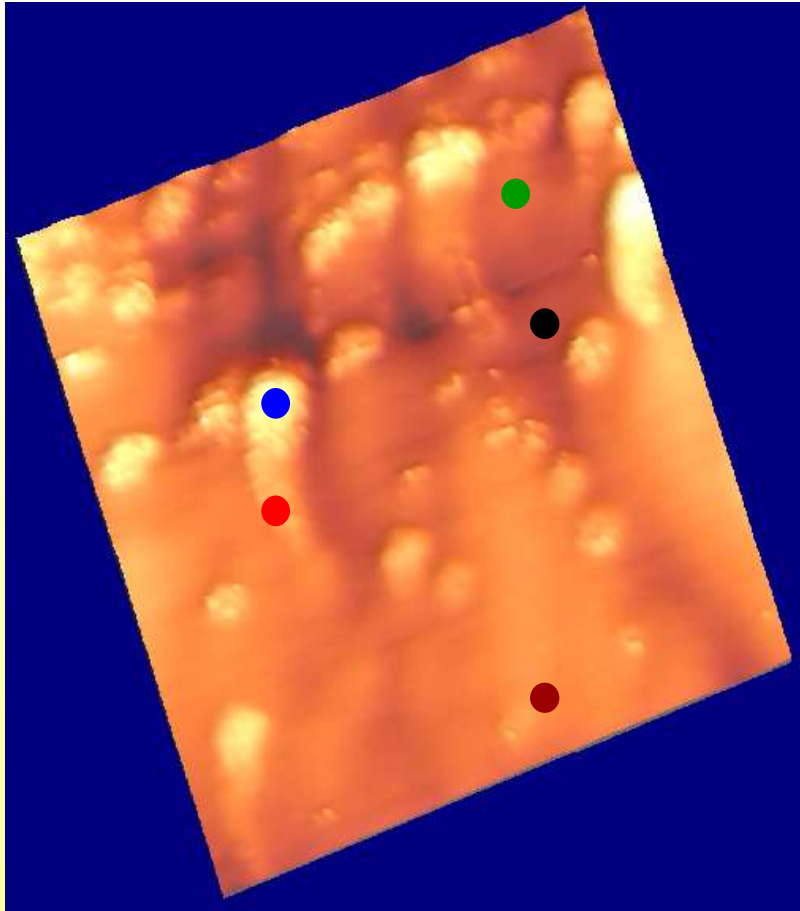


Electrostatic force spectroscopy on  $\text{Li}_2\text{O} \cdot \text{Al}_2\text{O}_3 \cdot 2 \text{SiO}_2$  glass ceramics



# Glass ceramic with 78% crystallinity

444 nm x 444 nm



High relaxation strength: large amount of glassy phase  
Low relaxation strength: large amount of crystalline phase

# Acknowledgements

## Collaborators:

Dr. Sevi Murugavel:  
Prof. Andreas Heuer  
Prof. Rudolf Friedrich

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Dr. Andre Schirmeisen  
Dr. Hartmut Bracht  
Ahmet Taskiran  
Dr. Sevi Murugavel  
Frank Natrup

} Electrostatic force spectroscopy

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